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Libration induced stretching mode excitation for pump-probe spectroscopy in pure liquid water

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We developed an experimental approach to study pure liquid water in the infrared and avoid thermal effects. This technique is based on libration induced stretching excitation of water molecules. A direct correspondence between frequencies within the libration and OH stretching bands is demonstrated. Energy diffusion is studied in pure liquid water by measuring wave packet dynamics of OH stretching vibrator with infrared femtosecond spectroscopy. Wave packet dynamics reveals ultrafast energy dynamics and reflects 130 fs intermolecular energy transfer between water vibrators. Energy diffusion is almost two orders of magnitude faster than self diffusion in water. © 2004 American Institute of Physics. [DOI: 10.1063/1.1800952]

I. INTRODUCTION

Liquid water plays a central role in chemistry and profoundly influences all molecular interactions in biological systems. The mechanisms of energy transfer in liquid water are essential for the understanding of a broad range of phenomena such as acid-base reaction, solvation, ionic channels, or protein folding. For a decade, H$_2$O molecule has been extensively studied by pump-probe techniques on a femtosecond time scale, often as an impurity in D$_2$O (HDO/D$_2$O), or in CCl$_4$. These experiments consist in following in time a vibrationally excited wave packet. Evolution of the amplitude and frequency of this wave packet yields information on the energy relaxation as well as on the hydrogen bonding network. Even though the geometrical properties of water (translation, rotation) are similar in these various configurations, pure water is nevertheless different from these systems as it is expected to exhibit resonant intermolecular energy transfer which precludes the local mode vibrators. Energy diffusion is almost two orders of magnitude faster than self diffusion in water.

A direct excitation in this region implies performing the experiments on very thin samples and induces problematic thermal effects. However, the spectrum also shows an interesting combination band around 2800 cm$^{-1}$, involving transitions from libration $\nu_L$ to stretching modes $\nu_{OH}$. Low frequency modes are dominated by translational modes (hydrogen bond stretching) below 200 cm$^{-1}$ and libration modes (hindered rotations) around 700 cm$^{-1}$. The transition $\nu_L \rightarrow \nu_{OH}$ corresponds to a transition from a libration “hot band” to the stretching band. Therefore it only involves water molecules which are in an excited libration mode. The probability to find a molecule in such an excited state decreases with energy according to Boltzmann distribution $p \propto \exp(-\Delta E/kT)$. At room temperature, this probability is a few percent, implying that the $\nu_L \rightarrow \nu_{OH}$ transition is allowed for a restricted number of water molecules. The idea is to excite the stretching OH vibrators by a pump pulse tuned at the difference of frequencies between libration and stretching modes. As a result, the libration mode induced absorption “dilutes” the pump excitation like in HDO/D$_2$O systems, but conserves the geometrical and resonant characteristics of pure water. The evolution of the excited molecules is then monitored by probing the ($\nu_{OH}=1 \rightarrow \nu_{OH}=2$) transition whose cross section is much stronger than the ($\nu_L=1 \rightarrow \nu_{OH}=1$) transition.

A fundamental issue for studying pure water dynamics is the possibility to select a subset of water molecules as this is currently done in HDO/D$_2$O systems. In order to achieve such a selection, the hot-band transition frequency $\nu_L \rightarrow \nu_{OH}$ must display a one to one correspondence with the stretching frequency $\nu_{OH}$. No strong structure is observed near 2800 cm$^{-1}$ in the linear spectrum of water because the band is wide and relatively close to the stretching modes. Then further modelization and analysis are required to justify this statement. We want now to address this question by investigating more carefully the libration modes of water molecules. Let us first consider the libration modes and their interaction with the environment. This coupling has been
In the midinfrared, the linear absorption spectrum of H$_2$O is dominated by three peaks: the symmetric and antisymmetric stretching modes $v_{OH}$ around 3300 cm$^{-1}$, the bending mode $\delta_{OH}$ at 1640 cm$^{-1}$ and a combination band between the bending and libration modes ($\delta_{OH} + \nu_L$) around 2200 cm$^{-1}$. Furthermore on the red side of $v_{OH}$, a combination band between $v_{OH}$ and libration modes extend from 2300 to 2900 cm$^{-1}$.

The libration frequency $\nu_L$ is related to $\beta$ by:

$$\nu_L = \frac{1}{4c}\beta \sqrt{\frac{3k_BT}{I}}.$$  

where $c$ is the light velocity, $k_B$ the Boltzmann constant, $T$ the temperature, and $I = 1.483 \times 10^{-40} \text{g cm}^2$ the inertial moment of the molecule. The angle $\beta$ relies on the molecular density by.

![Figure 1](image1.png)

**FIG. 1.** The linear absorption spectrum of H$_2$O in the midinfrared is dominated by three peaks: the symmetric and antisymmetric stretching modes $v_{OH}$ around 3300 cm$^{-1}$, the bending mode $\delta_{OH}$ at 1640 cm$^{-1}$ and a combination band between the bending and libration modes ($\delta_{OH} + \nu_L$) around 2200 cm$^{-1}$. Furthermore on the red side of $v_{OH}$, a combination band between $v_{OH}$ and libration modes extend from 2300 to 2900 cm$^{-1}$.

Studied in detail by Gaiduk and Gaiduk,$^{12}$ the model is the following. The libration bands are due to reorientation of the dipole moment of the water molecule as a whole in the hydrogen bonding network [Fig. 2(a)]. The water molecule moves in a rectangular potential profile with the depth $U_0$ and angular width $2\beta$ [Fig. 2(b)]. The reorientation is described by the hindered rotation angle $\beta$, which accounts for the interaction with the surrounding molecules and then depends on the hydrogen bonding density that hinders the molecular rotation. Molecules with energy $H < U_0$ perform libration, and molecules with $H > U_0$ perform free rotation. The libration frequency $\nu_L$ is then related to $\beta$ by:

$$\nu_L = \frac{1}{4c}\beta \sqrt{\frac{3k_BT}{I}}.$$  

where $\beta = \frac{\pi}{8} \sqrt{\frac{m_H M}{I} \left( \frac{M}{N_A\rho(T)} \right)^{1/3}}$, where $m_H$ is the proton mass, $M$ the molecular weight, $N_A$ the Avogadro’s number, $\rho$ the density, and $\sigma = 2.9$ A the effective diameter of the molecule. The frequency $\nu_L$ is therefore directly correlated to the average nearby hydrogen bonding length $R_{OH}$: a dense (loose) hydrogen bonding network is then responsible for high (low) frequency libration modes. The density is related to the average hydrogen bonding distance $R_{OH}$ by $\rho = C/R_{OH}^2$. At thermodynamical equilibrium, $C = 2.035 \times 10^{-23}$ g. Equation (1) then becomes:

$$\nu_L = \frac{136.3}{1.135} \frac{R_{OH}[\text{Å}]}{R_{OH}[\text{Å}]}.$$  

Furthermore, it is well known that the average stretching vibration frequency $v_{OH}$ is also correlated to $R_{OH}$.$^{14}$ Even though a dispersion exists in the relationship between $v_{OH}$ and $R_{OH}$,$^{15,16}$ the pump induced wave packet can be described by the average value of this dispersive relationship. Therefore, to a given hydrogen bonding network corresponds an average libration and stretching frequency. In order to address this point more quantitatively, we have carried out quantum mechanical calculation of the first and second stretching mode frequencies by solving a one-dimensional Schrödinger equation for the O-H coordinate $R_{OH}$ using an anharmonic Lippincott-Schröder potential.$^{17}$ This calculation shows that both ($v_{OH} = 0 \rightarrow v_{OH} = 1$) and ($v_{OH} = 1 \rightarrow v_{OH} = 2$) transition frequencies increase when $R_{OH}$ increases. The structure of the librational and vibrational levels, as depicted in Fig. 3, allows one to understand that $\nu_{pump} = v_{OH} + \nu_L$ displays a one to one correspondence with $v_{OH}$ and $\nu_L$.

![Figure 2](image2.png)

**FIG. 2.** Libration model for liquid water (from Ref. 12). (a) A water molecule is linked to four neighbors by hydrogen bonding (doted lines) and oscillates in the hydrogen bonding network with an angular amplitude $2\beta$. (b) The molecule evolves in a rectangular potential profile, with an angular width $2\beta$ and depth $U_0$.

![Figure 3](image3.png)

**FIG. 3.** Mode levels involved in the pump-probe scheme. The pump populates the first stretching mode from the first exited libration mode ($\nu_L = 1 \rightarrow v_{OH} = 1$). A pump at 2800 cm$^{-1}$ (respectively, 2600 cm$^{-1}$) excites the first stretching mode at an energy of about 3550 cm$^{-1}$ (respectively, 3380 cm$^{-1}$). Due to cross section consideration, the probe reads the second transition ($v_{OH} = 1 \rightarrow v_{OH} = 2$) starting at 3260 cm$^{-1}$ (respectively, 3060 cm$^{-1}$). After excitation, the wave packets evolve in both cases back to thermodynamical equilibrium at 3250 cm$^{-1}$ which the probe reads at 2960 cm$^{-1}$.
...therefore allows selective excitation of a stretching mode wave packet. The experimental principle is depicted in Fig. 3. At thermodynamical equilibrium, $v_L = 720 \text{ cm}^{-1}$ and $v_{OH} = 3250 \text{ cm}^{-1}$ corresponding to a transition frequency $v_L \rightarrow v_{OH} = 2530 \text{ cm}^{-1}$. An intense laser pulse tuned above the latter frequency creates an excited wave packet which will evolve back to the equilibrium position, revealing the dynamics of liquid water, as observed in Fig. 3. For instance, a pump pulse tuned at 2800(2600) cm$^{-1}$ creates an excited wave packet 270(70) cm$^{-1}$ above the equilibrium frequency.

The question of probing this excited wave packet must now be addressed carefully because a four-level quantum system is implied. From the first excited state $v_{OH} = 1$, three transitions are available: to the ground state ($v_{OH} = 1 \rightarrow v_{OH} = 0$, bleaching), to the second excited state ($v_{OH} = 1 \rightarrow v_{OH} = 2$, induced absorption) or back to the libration state ($v_{OH} = 1 \rightarrow v_L$). The resonance of $v_{OH}$ mode is 3250 cm$^{-1}$, with an anharmonicity of 300 cm$^{-1}$ toward the lower frequencies. Thus, the effect of bleaching of the transition is totally negligible compared to induced absorption in the 2600–3000 cm$^{-1}$ range which is covered by our probe. The contribution of transition back to the libration state may be estimated from the $v_{OH} = 1 \rightarrow v_L$ transition cross section. From the linear absorption spectrum and taking into account the reduced population of the libration modes, this latter is found to be at least four times weaker than the induced absorption one in the 2600–3000 cm$^{-1}$ range. The $v_{OH} = 1 \rightarrow v_L$ transition should therefore scarcely contribute to the pump-probe signal. In conclusion, one expects the pump-probe differential signal to be strongly dominated by the $v_{OH} = 1 \rightarrow v_{OH} = 2$ transition, implying an increase of the absorption of the probe induced by the pump.

III. EXPERIMENTAL SETUP

To perform pump-probe hole burning experiments in the midinfrared range, energetic laser pulses are required. The central element of the infrared laser source is a titanium:sapphire amplifier, delivering 130 fs pulses at 800 nm with a repetition rate of 1 kHz. It drives two lines of pulses independently tunable in the midinfrared. The principle of the generation is the parametric amplification of a quasicontinuum in the near infrared, followed by a frequency mixing in the midinfrared. The features of the sources are as follows. The more energetic line (the pump) has a duration of 150 fs and a spectral width of 65 cm$^{-1}$. It delivers more than 10 \mu J between 2800 and 3800 cm$^{-1}$. The independently tunable weaker line (the probe) has similar characteristics but with a maximum energy ten times less. The delay between the pump and the probe is precisely controlled by a computer. The sample cell is 40 \mu m thick and contains pure water at room temperature. The sample is circulated to avoid heating problems. The pump and the probe beams are focused in the sample by two 25 mm-focal length calcium fluoride lenses. The angle between the pump and the probe beams is 15°. In order to reduce the noise perturbation, the probe signal is normalized by the signal issued from a small part of the probe beam reflected before the cell. Furthermore, the pump beam is chopped at half the repetition rate of the laser (i.e. 500 Hz), in order to obtain successively a probe signal with and without the pump. With this procedure, we achieve signal to noise ratio of $10^4$. For a given pump frequency, differential spectra are recorded by tuning the probe frequency for several pump-probe delays.

IV. EXPERIMENTAL DATA

We now present differential spectra, that is, probe absorption with the pump minus probe absorption without the pump. The pump frequency is tuned at 2800 cm$^{-1}$ and the probe frequencies cover the range 2600–3000 cm$^{-1}$. The frequencies above 3000 cm$^{-1}$ are experimentally unobservable because of high absorption of water. The differential spectra are presented in Fig. 4. First, one notices an overall increase of absorption in presence of the pump, showing that induced absorption from first to second stretching excited state ($v_{OH} = 1 \rightarrow 2$) is the dominant contribution for the different spectra. Second, short delay spectra (−10 and 40 fs delays) show no evidence for spectral substructure around 2800 cm$^{-1}$, indicating that $v_{OH} = 1 \rightarrow v_L$ transition is totally negligible. As expected, these differential spectra are the signature of the wave packet evolution of the $v_{OH} = 1$ state, probed through $v_{OH} = 1 \rightarrow 2$ transition, because other transitions ($v_{OH} = 1 \rightarrow v_L$ and $v_{OH} = 1 \rightarrow 2$) are negligible. The time evolution of the spectrum shape is related to energetic reorganization of the wave packet under the influence of other water molecules and hydrogen bonding network. More precisely, in Fig. 4, for short delays, the spectra exhibit a maximum beyond 3000 cm$^{-1}$ which will be clarified further. This maximum clearly moves toward lower frequencies and stabilizes around 2900 cm$^{-1}$ after a delay of 200 fs. Simultaneously, the energy integral of the spectra decreases very rapidly with a dynamics of less than 200 fs. The energy is maximum for a delay of about 100 fs, and has almost completely relaxed 200 fs later. This shows a very fast dynamics of the energy stored in the excited wave packet, as well as the energetic reorganization of the wave packet. Both exhibit characteristic times less than 200 fs.
More precise information may be extracted from the data. Due to incomplete information of the differential spectra at short delays, Gaussian fit is not directly applicable. Indeed, a far and energetic wave packet will have roughly the same truncated spectral shape as a less energetic but closer wave packet. However, at longer delays, the shape of the wave packet allows us to extract energy and position with precision. From the knowledge of energetic evolution at delays longer than 100 fs, deduction of short delays dynamics is then possible. Evolution of the wave packet energy has been calculated and our data yields a dynamics of 110 cm$^{-1}$, which is in agreement with the model. As expected, one observes a far and energetic wave packet will have roughly the same truncated spectral shape as a less energetic but closer wave packet. However, at longer delays, the shape of the wave packet allows us to extract energy and position with precision. From the pump-probe correlation measurement, one can estimate the delay precision to be less than 20 fs. The second point is made possible by precisely synchronizing the pump and the probe in a GaSe nonlinear crystal for each couple of pump and probe frequencies to avoid small fluctuation of delays during the probe tuning.

From the pump-probe correlation measurement, one can estimate the delay precision to be less than 20 fs. The second point is clearly demonstrated in Fig. 5 by fits of the energy dynamics with characteristic times shorter (40 fs) and longer (200 fs), which can be discriminated from best fit, and provides the estimation for the fitting precision. The last point is the absence of optical coherent effects in the experiment, as pointed out by several other experiments on water. The calculated energy of the wave packet at short delays, Gaussian fit provides the position of the wave packet with good precision. The result is depicted in Fig. 6. As expected, the central position of the wave packet evolves from higher to lower frequencies. The amplitude of the displacement is important: about 220 cm$^{-1}$. Indeed, the wave packet moves on more than half of the width of the OH vibrator. At short delays, the wave packet position moves slightly from the starting point around 3180 cm$^{-1}$, because the pump is still generating the excited wave packet. Once the pump disappears, the wave packet evolves surprisingly quickly, being back to an equilibrium position in less than 300 fs. The origin around 3180 cm$^{-1}$ is associated with the probing of the $v_{OH}=1\rightarrow 2$ transition, corresponding to a $v_{OH}=0\rightarrow 1$ transition of 3495 cm$^{-1}$. It should be noted that error bars are relatively large at short delays. It comes from the uncertainty of the fitting procedure due to incomplete spectral bands. However, it does not question the observation of spectral diffusion in pure water because the fits are based on precise wing shapes and energy knowledge. An other set of experiments have been performed with the pump frequency tuned at 2600 cm$^{-1}$, that is, to say closer from thermodynamical equilibrium position. As expected, one observes (see Fig. 6) a spectral displacement similar to the one obtained with the pump at 2800 cm$^{-1}$. The starting point of the wave packet is lower, around 3060 cm$^{-1}$ and the amplitude is less important: 100 cm$^{-1}$. The equilibrium position is once again at 2920 cm$^{-1}$. Excitation at 2800 cm$^{-1}$ (respectively 2600 cm$^{-1}$) provides a wave packet centered around 3180 cm$^{-1}$ (respectively 3060 cm$^{-1}$), in good agreement with our model, and shows the nature of the libration-stretching coupling. A pump at higher frequency selects a subset of water molecules with larger average hydrogen bond length (see Fig. 3) due to both the increase of the stretching frequency and decrease of hot libration frequency with respect to $R_{O\cdots O}$. This also explains why moving the pump frequency 200 cm$^{-1}$ only moves the wave packet 120 cm$^{-1}$, in agreement with the model.

V. MODEL AND DISCUSSION

To extract quantitative information from the experimental data, we computed the behavior of the wave packet in spectral diffusion regime which requires the spectral diffusion characteristic time $\tau_{\text{diff}}$ as only dynamical parameter besides the pump and probe pulse duration. The best agreement, shown in Fig. 6, has been obtained with a characteristic time $\tau_{\text{diff}}$ equal to 110$\pm$15 fs. It should be noted that the
parameters used to fit the wave packet displacements for the two pump frequencies at 2800 and 2600 cm$^{-1}$ are the same, except of course for the amplitude of the displacement. The dynamics of the wave packet is once again shorter than the pulse duration. However the high precision obtained comes from the taking into account of the whole spectrum. Thus small spectral displacement and fast dynamics are easily discernible.

The physical origin of this spectral displacement may now be discussed. By analogy with solvatochromism found in HDO/D$_2$O, the first hypothesis would be to attribute this displacement to hydrogen bonding reorganization. The associated dynamics implies two time scales with approximately the same amplitude: a long time of about 700 fs (Ref. 1, 3) for hydrogen bonding network reorganization, and a short time of less than 100 fs related to the coherence loss of the vibrator through a single hydrogen bonding and which requires photon-echo type measurements. The measured time scale of 110 fs is far too short to support this hypothesis as hydrogen bonding network reorganization in pure water is very similar to the one in HDO/D$_2$O. Furthermore, our experiment is very similar to previous ones on HDO/D$_2$O, except of course the excitation principle. If this hypothesis was valid, we should have obtained the long time component due to network reorganization which is not the case. Another possibility might be related to intermolecular dynamics between $\nu_{\text{OH}}$ and $2\delta$ modes. However Raman experiments showed no evidence at all for such a transfer, and the spectral separation between the two modes seems too large to support a vibrational transfer of 110 fs. Vibrational Stokes shift can neither explain our results. It has been found equal to 70 cm$^{-1}$, but its amplitude is too small compared to 220 cm$^{-1}$. Furthermore, it is independent on the excitation frequency, thus pumping at 2600 and 2800 cm$^{-1}$ would lead to redshifts of equal amplitude, in contradiction with experimental results. Actually, the main difference between pure water and HDO/D$_2$O is that in pure water, a water molecule is surrounded by about four other similar water molecules. Vibrational energy transfer (VET) has therefore to be taken into consideration. Through VET, vibration from an excited water molecule diffuses to neighboring molecules, quickly altering the environment of the probed vibrator. Such VET has already been observed by Woutersen and Bakker simulated VET in pure water, and found a time transfer from 80 to 250 fs, in very good agreement with our data. This allows us to depict the model of diffusion in pure water as follows: the pump pulse, via libration modes, excites $\nu_{\text{OH}}$ vibrator at a given frequency. Each excited molecule is linked to four other water molecules by hydrogen bonding, which is a very good vibrational energy transfer vector. Neighboring vibrators are then progressively perturbed by successive hopping of energy. Their environment being different from the initial vibrator, their frequencies are changed accordingly. From vibrators excited above the equilibrium frequency as in our experiments, the wave packet frequency moves back to equilibrium position with very high speed, much more rapidly than the hydrogen bonding network reorganization. From this hopping diffusion process, one can attempt to access the energy diffusion coefficient in pure water. It depends on the number of hops required to investigate the whole geometrical conformations and is directly linked to the loss of geometrical correlation between water molecules. Radial distribution $R_{\text{DO}}$ in water shows that correlation is lost after the second shell surrounding the reference molecule. From that we estimate the hopping distance to be the mean OO distance between water molecules $l=0.285$ nm, with a hopping time equivalent to the measured diffusion time, $\tau=100$ fs. Einstein’s relationship $D = l^2/6\tau$ gives a diffusion constant $D = 1.4 \times 10^{-3}$ cm$^2$/s, which is 60 times faster than self-diffusion coefficient in water.

VI. CONCLUSION

This study shows that the response of pure water to an environmental change is strongly influenced by ultrafast energy transfer, with a characteristic time of about 100 fs. Resonant intermolecular energy transfer between water molecules seems to be the dominating process, even though intramolecular energy transfer between symmetric and asymmetric stretching modes could play a role. Resonant energy transfer in pure water needs to be taken into account in numerical simulations, such as proton transfer and water-protein interaction. Further theoretical models and numerical simulations of pure water are required to get a precise picture of the multiple modes found in pure water.

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