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Key Points:

- Observations show the importance of non-orographic waves at mid-latitudes
- Idealized simulations explain some of the observed gravity waves near jets
- Remaining challenges include taking moist processes into account

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Internal gravity waves from atmospheric jets and fronts
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Abstract For several decades, jets and fronts have been known from observations to be significant sources of internal gravity waves in the atmosphere. Motivations to investigate these waves have included their impact on tropospheric convection, their contribution to local mixing and turbulence in the upper troposphere, their vertical propagation into the middle atmosphere, and the forcing of its global circulation. While many different studies have consistently highlighted jet exit regions as a favored locus for intense gravity waves, the mechanisms responsible for their emission had long remained elusive: one reason is the complexity of the environment in which the waves appear; another reason is that the waves constitute small deviations from the balanced dynamics of the flow generating them; i.e., they arise beyond our fundamental understanding of jets and fronts based on approximations that filter out gravity waves. Over the past two decades, the pressing need for improving parameterizations of nonorographic gravity waves in climate models that include a stratosphere has stimulated renewed investigations. The purpose of this review is to present current knowledge and understanding on gravity waves near jets and fronts from observations, theory, and modeling, and to discuss challenges for progress in coming years.

1. Introduction

Internal gravity waves are waves occurring in the interior of a stratified fluid, with buoyancy providing the restoring force which opposes vertical displacements. Such waves are ubiquitous in the atmosphere and ocean and are the internal counterpart to the familiar surface gravity waves. In the atmosphere, they have horizontal scales ranging typically from 10 to 1000 km, and intrinsic frequencies bound between the Coriolis parameter and the Brunt-Väisälä frequency [e.g., Holton, 1992]. The highest intrinsic frequencies occur for displacements that are nearly vertical, and corresponding waves generally have shorter scales (simply reflecting that the forcing at high frequencies occurs at shorter scales). Amplitudes of internal gravity waves (or simply gravity waves (GWs)) generally are relatively small in the troposphere and stratosphere, in the sense that the flow at large scales (synoptic and larger) remains close to geostrophic balance, which excludes gravity waves. Based on the approximation that the flow is balanced, models have been derived, such as the quasi-geostrophic model, which simplify the dynamics and filter out gravity waves by construction. Most of our fundamental understanding of midlatitude dynamics comes from such balanced models [e.g., Vallis, 2006]. For example, baroclinic instability was identified with the development of the quasi-geostrophic approximation [Charney, 1947, 1948; Eady, 1949] and frontogenesis with that of a higher-order approximation, semigeostrophy [Hoskins and Bretherton, 1972]. Nonetheless, gravity waves can be of importance and reach large amplitudes locally, and their importance grows as we move up into the middle atmosphere (i.e., the stratosphere and mesosphere) [Andrews et al., 1987] and into the thermosphere. Indeed, as they propagate vertically and transfer momentum and energy from their origin (generally in the troposphere) to the level where they dissipate, they contribute to the circulation and variability in the stratosphere and force the reversal of the meridional thermal gradient in the mesosphere [Fritts and Alexander, 2003]. Furthermore, their dissipation may act as a source of secondary waves with impacts in the thermosphere [Oyama and Watkins, 2012].

General circulation models (GCMs) that include a middle atmosphere generally do not have sufficient resolution to describe gravity waves explicitly and hence need parameterizations to represent their main effects, namely, the forcing due to the deposition of momentum where the waves are dissipated [Kim et al., 2003]. One major difficulty with present parameterizations of gravity waves is the specification of their sources, which can be an arbitrary, tunable parameter due to lack of physical understanding and observational constraints.
The main sources of gravity waves include orography, convection, and jet/front systems. Flow over orography has long been known and studied as a source [e.g., Queney, 1948; see also references in Gill, 1982]. The importance of this source comes out strikingly in global assessments because many gravity wave hotspots are tied to orographic features [Hoffmann et al., 2013]. Nonorographic waves are nonetheless also important. First, the distributions of these sources are more spread out, with convection dominating in the Tropics, and jets and fronts dominating in the midlatitudes. Though locally less intense than some orographic sources, the integrated contribution of nonorographic waves can be comparable to those of orographic waves [Hertzog et al., 2008]. Second, the phase speeds of the former differ considerably from those of orographic waves, which matters crucially for the way these waves force the middle atmosphere [Andrews et al., 1987].

For convectively generated waves, several mechanisms have been proposed over the past two decades to explain waves generated by moist convection [Clark et al., 1986; Fovell et al., 1992; Alexander et al., 1995; Lane et al., 2001], paving the way for their parameterizations in general circulation models. Jets and fronts are known to be a major source of gravity waves, as shown by observations which have highlighted a conspicuous enhancement of gravity wave activity in the vicinity of jets and fronts [e.g., Fritts and Nastrom, 1992; Eckermann and Vincent, 1993; Plougonven et al., 2003]. In addition, numerous case studies have analyzed the occurrence of strong gravity wave events in the vicinity of a jet/front system. These case studies have isolated specific flow configurations: intense gravity waves of low frequency have repeatedly been identified in the exit region of jets in the upper troposphere, often upstream of a ridge of geopotential [Uccellini and Koch, 1987; Guest et al., 2000]. Such waves of low frequency are often called inertia-gravity waves.

However, the exact mechanisms through which the waves are generated near jets and fronts remain an active area of current research and debate. Candidate mechanisms associated with jet-front wave generation have included geostrophic adjustment, Lighthill radiation, unbalanced instabilities, transient generation, shear instability, and convection.

Several of these can be considered examples of spontaneous emission [Ford et al., 2000], i.e., emission of gravity waves by a flow that initially was well balanced (e.g., in geostrophic balance). This highlights one reason for the slow progress in understanding waves generated by jets and fronts: the latter are mainly understood in balanced approximations which by construction filter out gravity waves. Predicting gravity waves that appear in flows which, at some initial time, were arbitrarily close to balance amounts to determining the limitations of these balanced approximations [Vanneste, 2013]. Recent years have brought significant progress in the understanding of mechanisms of spontaneous emission. Analytical studies have described Lighthill radiation, unbalanced instabilities, and transient generation in simple flows and have provided asymptotic formulae quantifying the emitted waves [Vanneste, 2008].

With advances in computational power, it has been possible to complement these studies with idealized simulations that describe flows of realistic complexity, starting with O’Sullivan and Dunkerton [1995]. The simulated flows consist in the development and saturation of the instability of a midlatitude baroclinic jet [Thornicroft et al., 1993]. Gravity waves emitted in such simulations share features common with observational case studies. The background flow in which these waves appear is still quite complex (fully three dimensional, time evolving), so that even the origin of the waves is not always clear. A simpler flow has emerged as a paradigm that retains enough complexity (localized wind maximum, i.e., a jet streak) to produce analogous waves yet allow a quantitative explanation of their generation: it consists in a dipole (one cyclone and one anticyclone of similar size and amplitude) that propagates (quasi-)steadily [Snyder et al., 2007; Wang et al., 2009; Snyder et al., 2009; Wang and Zhang, 2010] and provides a clear paradigm for emission in jet exit regions [McIntyre, 2009]. These studies have underlined the role of the background flow on the waves that are generated and hence the importance of considering propagation effects.

This review will cover recent advances in many aspects of gravity waves from jets and fronts and discuss their impacts and importance. The review will complement the earlier review of Uccellini and Koch [1987] on observed gravity wave events associated with jet streaks and recent reviews of Fritts and Alexander [2003] on gravity waves and the middle atmosphere, of Kim et al. [2003] on gravity wave parameterizations, and of Richter et al. [2007] that summarized findings and discussions from a gravity wave retreat held at the National Center for Atmospheric Research in the summer of 2006.

The paper is organized as follows: observational evidence for the emission of gravity waves from jets and fronts is reviewed in section 2. Many different generation mechanisms have been proposed in relation to this problem. Mechanisms that have initially been pinned down through analytical developments, yield-
ing asymptotic results, are described first, in section 3. These theoretical results however do not connect straightforwardly to gravity waves observed in real flows. Understanding the generation and maintenance of gravity waves in more realistic flows requires a preliminary consideration of propagation effects (section 4). This allows us to consider in section 5 the emission in laboratory and numerical experiments, which occur in more realistic flows and which have led to a consistent explanation of certain gravity waves in jet exit regions. Impacts and parameterizations of waves generated from jets and fronts are presented in section 6. Our state of understanding and outstanding issues are discussed in section 7.

2. Observations

Broadly, observational studies of relevance can be separated into two categories: climatological studies which can describe, for example, the importance of storm tracks as source regions of gravity waves and case studies which provide specific examples of waves emitted from jets or fronts. Section 2.1 describes climatological studies, emphasizing those that quantify waves not only geographically but relative to the flow and in particular to jets and fronts. Section 2.2 describes case studies that specifically address the emission of gravity waves from jets and fronts. Finally, section 2.3 summarizes the limitations of observational studies regarding this issue and outlines challenges for years to come.

2.1. Climatological Studies

The following is organized by observational platform. We start with early studies using surface networks and climb progressively up to satellite observations. Climatological studies provide evidence for the importance of gravity waves from jets and fronts in several ways: at minimum, they may provide a suggestive seasonal cycle; at best, the intensity of gravity waves may be analyzed with respect to the background flow configuration.

Surface observational networks have been available for several decades and have provided the first opportunity for systematic climatological documentation and characterization of gravity waves [see Uccelini and Koch, 1987, and references therein]. A very comprehensive study of gravity waves using surface pressure observations was presented in Koppel et al. [2000] who examined the distribution of large hourly pressure changes (> 4.25 hPa) during a 25 year period over the United States. They found the most frequent occurrences of large-amplitude surface pressure changes are over the Great Plains (in the lee of the Rockies) and over New England (in the storm track and jet stream exit region). They also found that the large-amplitude gravity wave activity is more prevalent over winter and spring during the period of strong atmospheric baroclinicity [see also Grivet-Talocia et al., 1999]. Their composite analysis shows that the flow patterns are in broad agreement with the gravity wave paradigm of Uccelini and Koch [1987] (see section 2.2).

The radiosounding network provides useful information on gravity waves, when high-resolution measurements are recorded. In contrast to surface barographs, which give access to high-frequency waves affecting the lower atmosphere [Trexler and Koch, 2000], radiosondes can document waves up to the middle of the stratosphere, with more emphasis on low-frequency waves. Indeed, inertia-gravity waves have a particularly clear and informative signature in the hodograph. The analysis of the latter constitutes a standard tool for the estimation of gravity wave characteristics from vertical wind profiles [Sawyer, 1961; Hirota, 1984; Hirota and Niki, 1985].

Wang and Geller [2003] used the high vertical resolution radiosonde wind and temperature data to examine the gravity wave climatology over the United States during 1998–2001 (see their Figure 6). They found that the tropospheric and lower stratospheric gravity-wave energies are both stronger in winter than summer, likely owing to the presence of stronger baroclinic jet-front systems. Further investigations of the gravity wave field from high-resolution radiosonde observations above the United States used a ray tracing model to try and identify sources [Gong et al., 2008], leading to a better estimation of convective sources [Geller and Gong, 2010; Gong and Geller, 2010]. Radiosondes have also been analyzed in other regions, in particular when specific campaigns have made high-resolution profiles available. Sato and Yoshiki [2008] examined stratospheric gravity waves from 3-hourly radiosondes launched from Syowa station in Antarctica. Large and sporadic gravity wave activity was observed during the winter months, with some events of gravity waves generated from the polar night jet, and propagating upward and downward. Zhang and Yi [2007] have analyzed gravity waves in several years of twice-daily radiosondes, from several stations in China, and also found that the upper tropospheric jet was the main source of waves. More precisely, they suggest the strong wind shear induced by the jet as the source of waves [Zhang and Yi, 2005, 2008].
Radiosondes launched over the open ocean, far from land masses, provide valuable observations for quantifying nonorographic waves. Guest et al. [2000] have analyzed gravity waves in ozonesonde profiles reaching 30 km altitude over Macquarie Island, a small island of the Southern Ocean. Cases with strong inertia-gravity waves were analyzed and led to the identification of a common meteorological pattern: intense waves were found downstream of a jet streak, between the inflection point and the ridge of geopotential. Using ray tracing analysis, they confirmed that the waves observed in the lower stratosphere originated from a tropospheric jet-front system. Sato et al. [2003] made a meridional scan of gravity wave activity over the Pacific Ocean, from 28° N to 48° S with an interval of 1°. Gravity wave energy was maximized over the tropical region where convection is active and over the midlatitudes where the subtropical westerly jet is located. Plougonven et al. [2003] used soundings launched over the Atlantic Ocean during the Fronts and Atlantic Storm-Tracks Experiment (FASTEX) campaign (January–February 1997) [Joly et al., 1997] and also found gravity wave activity to be maximal in the vicinity of the jet stream [see also Moldovan et al., 2002]. More specific analysis led to identify two flow configurations for which intense gravity waves were present: the vicinity of a strong, straight jet and the jet exit region of a strongly curved jet, either in a trough [Plougonven et al., 2003] or in a ridge [Plougonven and Teitelbaum, 2003]. Only in the case of jet exit regions was it possible to carry out case studies of clear, intense inertia-gravity waves consistently identified in several soundings. The waves had frequencies between \( f \) and \( 2f \), wavelengths of a few hundred kilometers, wind perturbation of 5–8 m s\(^{-1}\), similar to Guest et al. [2000].

Aircraft measurements have also provided a means to quantify waves in different flow configurations, isolating jets and fronts as sources. Analyzing in situ measurements aboard commercial aircraft during 1978 and 1979, Fritts and Nastrom [1992] and Nastrom and Fritts [1992] attributed the mesoscale variance enhancements of horizontal velocity and temperature (presumably mostly induced by gravity waves) to four different sources: topography, frontal activity, nonfrontal convection, and wind shear. Overall, they found variances of temperature and wind at horizontal scales less than approximately 100 km to be 6 times larger in the vicinity of these sources than in a quiescent background, emphasizing the intermittency of gravity wave sources. The relative importance of the different sources was evaluated as shown in Figure 1, indicating strong values of variances above jets and fronts, smaller than those above topography by a factor of \( \sim 2 \) for wind speed and comparable for temperature.

Ultra-long-duration, superpressure balloons drift on isopycnic surfaces and behave as quasi-Lagrangian tracers, yielding a direct measurement of intrinsic frequencies which is very valuable for gravity wave studies.
of orographic origin, and regions without (oceans and the Antarctic Plateau). Integrating zonal momentum fluxes over each region separately, they showed that the overall contribution of nonorographic waves, although yielding locally weaker values, was comparable to or greater than that from orographic waves (see Figure 2). However, their analysis misidentifies certain waves: it has been shown that gravity waves due to the Andes or to the Antarctic Peninsula propagate on considerable distances downstream [Plougonven et al., 2010; Sato et al., 2012], and the regions used by Hertzog et al. [2008] did not extend more than a few hundred kilometers downstream of these obstacles. Complementary to this data analysis, Plougonven et al. [2013] have carried out mesoscale simulations (Δx = 20 km) of the flow above the polar cap for 2 months during the Vorcore campaign. A satisfactory quantitative agreement was found between the simulated and observed gravity wave momentum fluxes. Again, a regional decomposition was used, but the region of the Antarctic Peninsula extended much further downstream. This confirmed that the overall contribution from nonorographic waves was comparable to that of orographic waves for this domain and time, consistent with Hertzog et al. [2008]. The intermittency of the nonorographic waves was also quantified and contrasted with the much larger intermittency associated with orographic waves [Plougonven et al., 2013; Hertzog et al., 2012].

Besides the aforementioned in situ measurements, remotely sensed observations from ground-based radars, lidars, and airglow are also widely used to detect atmospheric gravity wave activity. Using observations from an ST (stratosphere-troposphere) radar during four extended observational campaigns in southern Australia, Eckermann and Vincent [1993] examined the generation of gravity waves from cold fronts. They found order of magnitude increases in mesoscale variance of winds attributable to gravity waves during frontal passages. They also found it possible to detect certain waves (in the upper troposphere, with long horizontal wavelengths and large ground-based phase speed) a day before and a day after the front’s arrival, whereas large amplitude, higher-frequency, shorter horizontal wavelength waves are directly associated with the onset of the frontal circulation at the surface.

Very High Frequency (VHF) clear-air Doppler radars are capable of making continuous measurements of the three-dimensional wind vector at high resolution in the troposphere, lower stratosphere, and mesosphere. This type of radar is called a mesosphere-stratosphere-troposphere (MST) radar or a stratosphere-troposphere (ST) radar depending on the observable height range primarily determined by the power-aperture product of the radar. The MU (middle and upper atmospheric) radar, an MST radar located at Shigaraki, Japan, has been providing measurements of gravity waves since 1984. Hirota and Niki [1986] identified, in a case study from one day of continuous measurements, inertia-gravity waves propagating upward and downward from the jetstream, clearly indicating the latter as the source of the waves. Sato [1994] examined gravity wave activity using wind data derived from this radar over 1986–1988 and found the dominant waves in the lower stratosphere tend to have short vertical wavelengths (~4 km) and long

Figure 2. Latitudinal distribution of zonal mean, density weighted absolute momentum flux carried by waves over orographic regions (thin solid), by waves over nonorographic regions (thin dashed), and by both types of waves (thick solid), as estimated by [Hertzog et al., 2008] from balloon observations.
An MST radar located in Aberystwyth, Wales, has been operated on a quasi-continuous basis since 1997. This MST radar was used for several case studies of inertia-gravity waves excited by jets and fronts [Pavelin et al., 2001; Pavelin and Whiteway, 2002] (see section 2.2). Vaughan and Worthington [2007] analyze inertia-gravity waves with 8 years of observation from this radar. They found inertia-gravity waves generally propagating upward in the lower stratosphere and downward in the troposphere, similar to Hirota and Niki [1986], evidence that the source is at the jet-stream level. Long period waves (>12 h) were not preferentially associated with a jet stream and showed little seasonal dependence, in marked contrast with shorter period waves (6–8 h) which were clearly associated with the jet and had a winter maximum. A seasonal cycle was also found in studies of stratospheric gravity waves from lidar measurements [Wilson et al., 1991; Murayama et al., 1994], but given the height of the measurements, this seasonality rather reflects the effects of propagation in the background winds (strong correlations were found between wave activity and wind speed).

Since Fetzer and Gille [1994] first used LIMS (Limb Infrared Monitor of the Stratosphere) measurements to estimate gravity waves, satellites have provided an increasing amount of information on the gravity wave field, on a global scale [e.g., Wu and Waters, 1996] and including estimations of momentum fluxes. Overall synthesis of such observations can be found in the recent review paper of Alexander et al. [2010] (see also Preusse et al. [2008] for a summary of the spatial and temporal resolution of different satellite based instruments). These satellite studies provide global distributions and hence some information on gravity waves generated from jets and fronts.

 Estimates of GW momentum fluxes or temperature variances have shown consistently, in different studies, enhanced values in the stratospheric winter polar night jet (e.g., Wu and Zhang [2004]; Wu and Eckermann [2008]; Alexander et al. [2008]; Yan et al. [2010]; Ern and Preusse [2011], see Figure 3). This can be interpreted as a signature of significant sources (orographic and nonorographic) in the winter midlatitudes but also as the signature of favored propagation within the positive shear of the strong stratospheric westerlies [Dunkerton, 1984; Sato et al., 2009; Ern and Preusse, 2011]. The zonal asymmetries are indications of enhanced sources and emphasize orography as a source at middle and high latitudes [Wu and Eckermann,
Interestingly, Wu and Eckermann [2008] use the different sensitivity of their instrument between ascending and descending orbits to show that waves in the midlatitudes have a preferred horizontal orientation, with phase lines extending from south-west to north-east in the Northern Hemisphere and from north-west to south-east in the Southern Hemisphere. This is consistent with the orientation of many tropospheric fronts, with the momentum fluxes estimated over the Southern Ocean from balloon observations [Hertzog et al., 2008] and with numerical simulations [Shutts and Vosper, 2011; Plougonven et al., 2013].

Numerical weather prediction (NWP) models are increasingly capable of resolving at least part of the gravity wave spectra in the troposphere and stratosphere in both their analyses and forecasts. Even at moderate resolutions, relevant information about the location and intrinsic frequency of gravity waves can be obtained [Plougonven and Teitelbaum, 2003; Wu and Zhang, 2004]. Wu and Eckermann [2008] compared monthly mean GW-induced temperature variances at 44 km pressure altitude derived from operational global analysis fields of the European Center for Medium-Range Weather Forecast (ECMWF) in August 2006 with those derived from satellite observations (Aura Microwave Limb Sounder (MLS), see Figure 3). At least part of the enhanced gravity wave activity over the Southern Ocean is related to strong baroclinic jet-front systems during this winter month. Schroeder et al. [2009] also found good agreement between gravity wave-induced temperature fluctuations derived from satellite observations (SABER, Sounding of the Atmosphere using Broadband Emission Radiometry) and the ECMWF analysis, including those at the edge of the winter polar vortex or the midlatitude jet streams.

More recently, Shutts and Vosper [2011] presented an in-depth comparison of the gravity wave fluxes derived from both the Met Office and ECMWF forecast models for August 2006 with those from the High Resolution Dynamic Limb Sounder (HIRDLS). They concluded that the state-of-the-art NWP models are capable of capturing the correct overall strength and distribution of gravity wave activity. Zhang et al. [2013] compared simulated gravity waves for month-long simulations over North America and the Atlantic with satellite observations and found a good agreement. They noted the sensitivity to the model spin-up time, consistent with the sensitivity study of Plougonven et al. [2010]. Plougonven et al. [2013] used observations from the Vorcore balloons [Hertzog et al., 2008] to systematically assess the realism of the gravity wave field in a mesoscale meteorological model (the Weather Research and Forecast Model) [Skamarock et al., 2008]. Relative to the observations, the simulations (with a horizontal resolution of $\Delta x = 20$ km) slightly underestimated nonorographic waves (factor $\sim 0.8$ for the time-averaged value).

### 2.2. Case Studies

In contrast to the climatological studies above, individual case studies typically isolate specific flow configurations in which intense gravity waves are unambiguously identified. Tropospheric jets and fronts were long hypothesized to be responsible for numerous observed gravity wave events, both in the troposphere [Tepper, 1951] and in the upper atmosphere above the tropopause [Hines, 1968]. However, given the limitations in the observing techniques, there were inherent uncertainties in the source attribution of these earlier observations [Hines, 1968; Gossard and Hooke, 1975]. Below we review case studies starting from the review of Uccellini and Koch [1987]. Whereas early studies emphasized tropospheric (ducted) waves, the focus over the last decade has shifted to upper tropospheric waves propagating into the stratosphere.

Uccellini and Koch [1987] (hereafter UK87) reviewed 13 long-lived observed lower tropospheric gravity wave events in the literature (see references therein). These mesoscale disturbances have wave periods of 1–4 h, horizontal wavelengths of 50–500 km, and surface pressure perturbations of 0.2–7 mb, all of which have been shown to influence the mesoscale structure of precipitation systems. They found a common synoptic environment for the generation and maintenance of these waves as being in the exit region of upper level jet streaks and cold-air side of a surface frontal boundary (Figure 4). They further hypothesized that these gravity waves are likely to be generated by the unbalanced upper tropospheric jet-front systems through geostrophic adjustment (see section 3.1) and to be maintained through wave ducting [Lindzen and Tung, 1976] (see section 4.1).

Case studies in the years following UK87 increasingly involved mesoscale numerical modeling. The earliest simulations of mesoscale gravity waves using numerical weather prediction models were conducted by Zhang and Fritsch [1988], Schmidt and Cotton [1990], and Cram et al. [1992]. Gravity waves in these studies were generated by the simulated mesoscale convective systems. However, detailed verification of these waves against mesoscale observations was not performed due to the unavailability of mesoscale data sets. Mesoscale numerical models have subsequently been developed into powerful tools available for the
Figure 4. Flow configuration identified by Uccellini and Koch [1987] (UK87) as conducive to intense gravity waves: lines of geopotential in the midtroposphere and surface fronts are indicated. Just downstream of the inflection axis (dashed line), the wind has a significant cross-stream ageostrophic component (wind vector crossing isolines of geopotential) and intense gravity waves are recurrently found (shaded region). Adapted from Koch and O'Handley [1997].

A detailed study of gravity wave structure, energy sources, and maintenance mechanisms, all of which are difficult to detect with standard observations.

The first published attempt to use a mesoscale model for the sole purpose of simulating and studying an observed gravity wave event, and for which verification was performed against detailed mesoanalysis, was provided by Powers and Reed [1993]. The case simulated was the long-lived, large-amplitude gravity wave event on 15 December 1987 over the Midwest of the U.S. [Schneider, 1990]. Powers and Reed [1993] concluded that the mesoscale NWP model used could successfully simulate mesoscale gravity waves and capture many aspects of the observed waves in terms of both timing and magnitudes. Although this event had characteristics of mesoscale gravity waves under typical synoptic settings as conceptualized by Uccellini and Koch [1987], the authors suggested the model waves were maintained and amplified by wave-CISK (Conditional Instability of the Second Kind) processes, through which moist processes and diabatic heating reinforce the internal waves [Lindzen, 1974]. Powers [1997] further concluded that elevated convection above a stable wave duct was the forcing mechanism in the model. Pokridentt et al. [1996], who studied the same case also with numerical simulations, on the other hand hypothesized that a transverse circulation about the approaching jet streak produced a mesoscale potential vorticity anomaly at midlevels that subsequently forced the mesoscale waves.

One of the cases reviewed in UK87 is the 11–12 July 1981 gravity wave event that is believed to be responsible for triggering and organizing mesoscale convection over southeast Wyoming into the Dakotas during the Cooperative Convective Precipitation Experiment (CCOPE) [Koch and Golus, 1988; Koch and Dorian, 1988; Koch et al., 1988, 1993]. There are at least two distinct wave episodes detected by the CCOPE high-resolution surface mesonet [Koch and Golus, 1988]. The synoptic-scale analysis in Koch and Dorian [1988] showed that the waves are confined to the region between the axis of inflection and the ridge in the 300 hPa height field, downstream of a jet streak and to the cold air side of a surface quasi-stationary front. There is also evidence of strong flow imbalance associated with the upper level jet from observational analysis [Koch and Dorian, 1988] and from mesoscale modeling [Kaplan et al., 1997]. Subsequent numerical simulations by Zhang and Koch [2000] and Koch et al. [2001] did simulate reasonably well the observed gravity waves. However, these latter studies concluded that despite the proximity of the wave generation with the jet streaks, the thermally driven mountain-plains solenoid circulation (MPS) is responsible for the generation of both wave episodes: the first through an orographic density current relegated from a remnant daytime MPS circulation [Zhang and Koch, 2000] and the second by convection triggered by the developing MPS, although the background jet may play a role in the wave propagation and maintenance [Koch et al., 2001].

The relevance of the UK87 paradigm has been highlighted in a number of other case studies and shown to be robust for the presence of waves [e.g., Ramamurthy et al., 1993]. Often it is found that the waves have an impact on convection and precipitation [Tremler and Koch, 2000; Richiardone and Manfrin, 2003], although the relation varies. This impact has been one motivation for the development of an automated system for predicting and detecting mesoscale gravity waves using surface observations [Koch and O'Handley, 1997; Koch and Saleeby, 2001]. Both studies suggest the hypothesis that the unbalanced flow in the jet streak exit region or near frontal boundaries is associated with mesoscale gravity wave generation.

Another well-studied case is the 1992 St. Valentine’s Day mesoscale gravity wave event observed during Stormscale Operational and Research Meteorology–Fronts Experiment Systems Test [Tremler and Koch, 2000;
Rauber et al., 2001]. High-resolution mesoscale NWP models had been used to simulate the event with varying degrees of success, while the mechanisms derived from different simulations differ greatly. Through unbalanced flow diagnosis of the model simulations, Jin [1997] and Koch and O’Handley [1997] believe this event followed closely the jet-gravity wave paradigm of UK87, though as in previous studies, Jin [1997] also finds convection is important for maintaining and amplifying the mesoscale waves. Through numerical experiments with and without evaporative processes, Jewett et al. [2003] singled out the importance of the evaporatively driven downdrafts impinging upon the surface warm-frontal inversion on the wave genesis.

Whereas observations alone have recurrently been insufficient to support conclusions on the relation of ducted gravity waves and convection [e.g., Ralph et al., 1993], high-resolution mesoscale simulations in complement to observations can provide key insights. A large-amplitude gravity wave event over the northeastern United States on 4 January 1994 was documented in Bosart et al. [1998] that showed wavelengths of 100–200 km and peak crest-to-trough pressure falls exceeding 13 hPa within 30 min associated with short-term blizzard conditions. The synoptic-scale pattern of this wave event is again consistent with the UK87 paradigm from the observational analysis. Through successful simulation of this event with a high-resolution mesoscale model, Zhang et al. [2001, 2003] demonstrated the radiation of the gravity waves to the lower troposphere from an unbalanced upper tropospheric jet streak. The wave packet emitted from the upper level jet streak subsequently merged with a midtropospheric cold-front aloft and triggered moist convection. A ducted wave-CISK mode was responsible for the subsequent wave maintenance and amplification. Hence, although moist processes were not at the origin of the wave, they played a crucial role to amplify it, as shown by dry simulations.

It is worth noting that a number of case studies fall outside the flow configuration of the UK87 paradigm. For example, Ralph et al. [1999] described gravity waves found ahead of a cold front, suggesting that the cold front plays the role of an obstacle to the flow impinging on it. The flow pattern in this case was significantly constrained by the presence of mountains to the West of the cold front, and further investigations would be necessary to determine whether this “obstacle effect” of cold fronts was exceptional or commonly occurs.

The above case studies have focused on tropospheric waves, their interactions with convection and their effects near the surface. Over the past three decades, more emphasis has been made on waves near the jet stream and into the stratosphere. Sato [1989] analyzed an inertia-gravity wave propagating downward from a turbulent layer in the upper level jet, in a pressure trough. The horizontal wavelength was estimated to be 300 km. Yamanaka et al. [1989] used radar measurements from an MST radar to carry out a case study of low-frequency waves above the jet stream. In an original analysis of the phase speeds of the waves, they showed that the waves propagating upward in the stratosphere had their origin in the upper level jet stream, not near the ground. The inertia-gravity waves analyzed had intrinsic frequencies of 3 to 4f, had vertical wavelengths between 1 and 3 km, and coincided with a maximum of the wind speed below.

The flow configuration identified by UK87 has also been found to be relevant for emission into the lower stratosphere. Guest et al. [2000] have highlighted the jet exit region of a jet streak approaching the inflection point between the base of a trough and a ridge as a configuration conducive to intense gravity waves in the lower stratosphere. Ray tracing was used to identify the origin of clear, intense inertia-gravity waves observed in the lower stratosphere and has highlighted the upper level jet as the region of emission [Guest et al., 2000; Hertzog et al., 2001]. Instances of generation from jets in a region a priori dominated by orographic waves were also documented by Spiga et al. [2008] combining reanalyses, satellite and radiosoundings data, and mesoscale model simulations. Tateno and Sato [2008] analyzed two stratospheric wave packets using intensive high-resolution radiosonde observations (10 high-resolution profiles over 27 h). A combination of ray tracing and of the ECMWF analyses showed that the likely source was the upper level jet, upstream by more than a day and more than 1000 km. High values of the Lagrangian Rossby numbers were found to coincide with this tentative source, suggesting that the waves are due to spontaneous adjustment processes (see section 3).

Case studies focusing on upper tropospheric and lower stratospheric observations have often emphasized the presence of both upward and downward waves from the jet as a clear signature of emission by the jet [Hirota and Niki, 1986; Sato, 1989; Thomas et al., 1999; Plougonven et al., 2003; Wu and Zhang, 2004; Spiga et al., 2008]. From 17 radiosoundings launched at 3 h intervals over Northern Germany, Peters et al. [2003] clearly identified inertia-gravity waves propagating upward and downward from the jet which amplified downstream of the jet streak. Complementing similar radiosonde observations with mesoscale simulations,
Figure 5. Comparison of gravity waves in satellite observations and in mesoscale simulations, from Wu and Zhang [2004]. (left) Radiance perturbations from different channels of the NOAA 16 AMSU-A at 0630 UT on 20 January, showing gravity wave perturbations at different heights. (right) Geopotential height (thick contours every 20 dam) and maxima of wind speed (shaded regions) at 300 hPa and 80 hPa horizontal divergence (every $3 \times 10^{-5}$ s$^{-1}$; blue, positive; red, negative) from the MM5 simulations at 1800 UT on 19 January (starting on 19 January at 0000 UT). Simulated amplitudes of wind and temperature perturbations are 10 m s$^{-1}$ and 5 K, respectively.

Zülicke and Peters [2006] identified, in a poleward-breaking Rossby wave, subsynoptic (horizontal wavelength $\lambda_h \sim 500$ km) and mesoscale waves ($\lambda_h \sim 200$ km). Their study provides further evidence that the flow conditions in the jet exit region are a key feature that leads to the common occurrence of waves there.

Wu and Zhang [2004] have carried out numerical simulations in complement to satellite observations of the Advanced Microwave Sounding Unit-A (AMSU-A). Waves from a baroclinic jet/front system were identified east of Newfoundland in both the radiance perturbations and the simulations, with a good level of agreement between the two (see Figure 5). They observed that gravity waves in this storm-track exit region, found in many winters, can reach the stratopause. Importantly, this is one of the first studies that directly linked the satellite-derived gravity wave activity with the intensity and location of the tropospheric baroclinic jet front systems.

First, systematic measurements of upper tropospheric and lower stratospheric gravity waves with a dedicated research aircraft were conducted during the 2008 field experiment of Stratosphere-Troposphere Analyses of Regional Transport (START08) [Pan et al., 2010]. During one of the research flights, accompanied with a strong baroclinic jet-front system across the continental United States, apparent activity of gravity waves at different scales near or just above the tropopause region was sampled over a distance of a few thousand kilometers. While research is still ongoing to examine the sources of these observed gravity waves, it is apparent that the tropospheric jet-front systems, in interaction with the local topography and moist convection, were playing essential roles in the forcing and characteristics of these gravity waves [Zhang et al., 2009].

Regarding generation mechanisms, case studies have often referred to geostrophic adjustment [e.g., Pavelin et al., 2001]. The justification is that observed and simulated GWs are often found in the vicinity or just downstream of regions of imbalance, with Lagrangian Rossby numbers serving as an indicator of imbalance [Koch and Dorian, 1988; Ramamurthy et al., 1993; Spiga et al., 2008]. A more sophisticated indicator is provided by the residual of the nonlinear balance equation [Zhang et al., 2000, 2001] and has been used efficiently [e.g., Hertzog et al., 2001]. However, the relation is merely a colocaction (the waves are found near a maximum of an indicator of imbalance), but it is not systematic (e.g., there are other maxima that are not associated with waves) and a quantitative relationship is still lacking.

2.3. Limitations and Challenges

Analyzing gravity waves from observations raises a number of issues and challenges. This is in part tied to the limitation of each observational platform, making it sensitive only to a certain portion of the gravity wave spectrum [Alexander, 1998; Preusse et al., 2008]. In addition, each method used to infer gravity waves from measurements comes with its limitations and uncertainties. For example, the commonly used hodograph method may give erroneous estimates of wave characteristics when the observed fluctuations result from a superposition of waves [Eckermann and Hocking, 1989; Zhang et al., 2004]. When sufficient
observational information is available, e.g., with radar data, it is possible to circumvent these limitations by estimating the same parameters with different methods and checking the consistency [e.g., Sato, 1994]. In complement, numerical simulations may contribute to estimating uncertainties [Zhang et al., 2004].

Nevertheless, observations have provided robust and substantial evidence for the importance of jets and fronts as sources of gravity waves and case studies have identified flow configurations favorable to the presence of significant waves. Two important limitations need to be mentioned: one is that observations identify where gravity waves are found, not necessarily where they are generated. Hence, favored locations may carry information on propagation effects, not only generation. Second, case studies may introduce a bias toward cases that lend themselves well to case studies, i.e., where conspicuous gravity waves (large amplitude, large enough scale and time span that the wave can be identified, say, in several radiosondes) that can be well identified and interpreted. Generally, perturbations that occur on smaller scales, and in particular those that are tied to moist convection, prove more difficult to interpret beyond statistical approaches [e.g., Fritts and Nastrom, 1992; Eckermann and Vincent, 1993; Plougonven et al., 2003].

A first challenge for gravity wave studies in general will be to make the different analyses of the gravity wave field converge [Alexander et al., 2010]. Comparisons of estimates from different satellites [Ern and Preusse, 2011], between satellites and analyses [Shutts and Vosper, 2011], between mesoscale simulations and balloon observations [Plougonven et al., 2013], or between observations and general circulation models [Geller et al., 2013] provide indications on the biases of these different sources of information and suggest that these different estimates may soon converge. A second and related challenge is to define and obtain a complete description of the useful characteristics of the gravity wave field: whereas mean momentum fluxes have very much been emphasized, they are not the only relevant quantity. For example, the intermittency of the wave field also matters, and this may be described through the probability distribution function of the momentum fluxes [Hertzog et al., 2012]. A third challenge consists in extracting information on the wave sources from a combination of observations and simulations. Investigation of the gravity wave field relative to the flow (both the tropospheric flow which may act as a source and the stratospheric flow which acts as a background) will be a path to help identify sources, going beyond geographical and seasonal variations. A final challenge concerns the role of moist processes in the vicinity of jets and fronts. As described above, a number of case studies have emphasized the role of moist processes in generating or amplifying waves near jets and fronts. Clarifying the contribution of moist processes to waves in the vicinity of jets and fronts is an important issue and calls for dedicated research efforts.

Despite the availability of near continuous four-dimensional model output, discrepancies between different modeling case studies of the same events highlight the difficulties in pinpointing the forcing and generation mechanisms. These difficulties have driven in part the need for more idealized simulations with simpler flow patterns, which will be described in section 5.

3. Generation Mechanisms: Analytical Results

This section and section 5 review theoretical studies of generation mechanisms that have been invoked to explain gravity waves in the vicinity of jets and fronts. The present section restricts mainly to analytical studies and hence simple flow configurations, allowing asymptotic results. This section is complemented, in section 5, by a review of studies for which laboratory or numerical experiments have been a necessary component, providing an examination of emission in more realistic flows.

The observational evidence for a strong enhancement of gravity waves in the vicinity of jet/front systems has been one motivation for investigations of dynamical mechanisms generating gravity waves from predominantly balanced features of the flow. Another fundamental motivation has been to identify the limitations of balanced approximations, i.e., to determine when the evolution of the flow, while remaining predominantly balanced, includes the spontaneous generation of gravity waves.

The fundamental difficulty for the emission is the scale separation between the slow balanced motions and the fast gravity waves, making it difficult for both types of motions to interact. The Rossby number measures this separation of timescales: balanced motions evolve on the advective timescale $L/U$, whereas the longest timescale for gravity wave motions is $1/f$, with $f$ the Coriolis parameter. Their ratio yields the Rossby number

$$Ro = \frac{U}{fL}$$

(1)
which is typically small for midlatitude flows. To a very good approximation, atmospheric and oceanic motions at small Rossby numbers are balanced; i.e., a diagnostic relation can be established between the wind and other variables. The simplest balance relation is geostrophic balance, but there are more accurate relations [e.g., Hoskins et al., 1985; Zhang et al., 2000]. Additionally, the flows near jets and fronts typically have aspect ratios justifying hydrostatic balance in the vertical [e.g., Vallis, 2006]. These balances provide diagnostic relations which reduce the number of time derivatives in the system: balanced approximations such as quasi-geostrophy provide a simple description of the balanced flow, consisting of an inversion relation and a single prognostic equation, the advection of the materially conserved potential vorticity [Hoskins et al., 1985]. Gravity waves have been filtered out. Balanced models have provided much of our understanding of midlatitude dynamics and are helpful for initialization issues in numerical weather forecasting [e.g., Kalnay, 2003]. The occurrence of gravity waves in the vicinity of jets and fronts constitutes a deviation from balance.

First, we describe geostrophic adjustment, because it has very regularly been invoked (section 3.1). Studies of geostrophic adjustment address how an initial imbalance projects onto gravity waves, but not the origin of the imbalance. The discussion on the relevance of geostrophic adjustment in the present context is deferred to section 7.1. Next, we describe explicit examples of spontaneous emission (or spontaneous adjustment emission, SAE), mechanisms explicitly addressing how gravity waves emerge from motions that are essentially balanced initially: Lighthill radiation (section 3.2), unbalanced instabilities (section 3.3), and transient generation (section 3.4). Further studies of spontaneous emission, in more realistic flows, are discussed in section 5. Finally, generation mechanisms involving shear instability are discussed in section 3.5.

### 3.1. Geostrophic Adjustment

Geostrophic adjustment occurs when a rotating fluid is forced away from a balanced state on timescales that are short relative to the inertial timescale. The process forcing the fluid away from balance need not be specified: for example, a wind burst forcing the upper ocean [Rossby, 1938], heating due to convection [Schubert et al., 1980], an absorbed gravity wave [Zhu and Holton, 1987], and mixing due to shear instabilities [Bühler et al., 1999] have been invoked. It only matters that this forcing be fast relative to the inertial timescale so that it can be considered instantaneous, yielding the classical initial value problem. More generally, this is only a special case of the adjustment to a time-dependent local body forcing [Weglarz and Lin, 1997; Chagnon and Bannon, 2005a]. Below, we reserve the term “geostrophic adjustment” for the classical initial value problem with geostrophy as the underlying balance.

The classical problem of geostrophic adjustment describes how an arbitrary initial condition, in a rotating fluid subject to gravity, splits into a geostrophically balanced part that remains and inertia-gravity waves which propagate away [Rossby, 1938; Cahn, 1945; Obukhov, 1949]. Rossby [1938] considered as an initial condition a rectilinear current in the upper layer of the ocean, with limited horizontal extent and with no surface height anomaly. Hence, the initial current is out of balance and the fluid adjusts so as to find a state in which velocity and pressure (here surface height) are in geostrophic balance and which preserve the potential vorticity and mass relative to the initial state. The excess energy contained in the initial condition is shed off, in the form of inertia-gravity waves that propagate away.

Studies on geostrophic adjustment have focused on configurations for which the problem is well posed:

1. If all motions are small perturbations to a state of rest, the adjustment can be described asymptotically in Rossby number [Blumen, 1972]. To leading order, the balanced part of the flow is described by quasi-geostrophic dynamics for Burger number of order unity [Reznik et al., 2001].
2. If the flow is zonally symmetric or axisymmetric, the separation is again unambiguous because the balanced part of the flow, even for large Rossby numbers, has a trivial time evolution: it is stationary. Adjustment has been investigated for purely zonal flows [e.g., Rossby, 1938; Yeh, 1949; Ou, 1984; Kuo and Polvani, 1997; Kuo, 1997; Zeitlin et al., 2003] and axisymmetric flows [e.g., Paegle, 1978; Schubert et al., 1980; Kuo and Polvani, 2000]. In both cases, the unambiguous separation made it possible to describe analytically nonlinear adjustment [e.g., Glendening, 1993; Blumen and Wu, 1995; Wu and Blumen, 1995; Plougonven and Zeitlin, 2005].
Note that in all cases, the initial imbalance is prescribed. The origin of this imbalance lies outside the scope of these studies. They only describe the response of the fluid, in certain limited configurations (small perturbations to a state of rest (1) or symmetric flows (2)).

Numerous aspects of the geostrophic adjustment problem have been studied, e.g., the dependence of the response to the scale of the initial perturbation [e.g., Matsumoto, 1961; Blumen and Wu, 1995; Kuo, 1997] or the interpretation of geostrophic adjustment as a minimization of energy for a given potential vorticity distribution [Vallis, 1992]. With the emission from jets in mind, Fritts and Luo [1992] have considered, in a stratified fluid at rest, initial imbalances having dimensions comparable with those of a jet stream. They found emitted waves that have low frequencies, consistent with the dispersion relation and the spatial scales of the prescribed imbalance. Their first, two-dimensional study was complemented by consideration of three-dimensional imbalances having long scales in the along-jet direction [Luo and Fritts, 1993].

In all of the examples above, the gravity waves originate from the initial, prescribed imbalance; hence, these examples provide little insight into the generation from balanced motions. The geostrophic adjustment problem was in fact used to investigate the interactions of gravity waves and balanced motions: in the first several orders of the asymptotic theory, Reznik et al. [2001] showed a complete decoupling of the balanced motions and gravity waves [see also Dewar and Killworth, 1995], yielding an unambiguous separation and hence no spontaneous emission [Zeitlin, 2008].

Now, various diagnostics of flow imbalance, as surveyed in Zhang et al. [2000], have been widely and successfully used to identify the sources of gravity waves with respect to the balanced flow [e.g., O’Sullivan and Dunkerton, 1995; Jin, 1997; Zhang et al., 2001]. In consequence, geostrophic adjustment has very often been referred to explain emitted waves near jets and fronts [e.g., O’Sullivan and Dunkerton, 1995]. In a related study of an idealized baroclinic life cycle, and in order to emphasize the differences with classical geostrophic adjustment, Zhang [2004] proposed the term balanced adjustment to describe the spontaneous generation of gravity waves from a predominantly balanced flow that continuously produces imbalance (as can be diagnosed from the residual of the nonlinear balance equation for example), with an associated, continuous emission of gravity waves. In order to avoid any confusion with a generalization of geostrophic adjustment that would simply include adjustment to higher-order balances than geostrophy (e.g., cyclogeostrophic balance) [see Holton, 1992], the term became “spontaneous balance adjustment” in Wang and Zhang [2010]. The investigation of this mechanism relies heavily on numerical simulations and will be described in section 5.

### 3.2. Lighthill Radiation

It is preferable to briefly recall the context in order to understand the change in paradigm between the previous section and the present one. The atmosphere and oceans are and remain so close to a balanced state on synoptic scales that the existence of a slow manifold [Lorenz, 1980; Leith, 1980] was suggested and investigated: within the phase space of the full equations, this would be an invariant subspace of reduced dimensionality containing only balanced dynamics (for more general definitions, see discussions in Warn et al. [1995] and Ford et al. [2000]). Investigating whether such a manifold exists is equivalent to investigating whether motions that are at one initial time purely balanced (or more precisely on the slow manifold) can produce, in the course of their evolution, unbalanced motions, i.e., gravity waves.

Several lines of evidence have progressively shown that such emission is inevitable, i.e., that an exactly invariant slow manifold in fact does not exist and that one should rather think of slow manifolds of various accuracies [Mackay, 2004; Vanneste, 2013, and references therein]. One line of evidence came from low-order models such as the Lorenz-Krishnamurty model [Lorenz, 1986; Lorenz and Krishnamurty, 1987] describing with five ordinary differential equations the interactions of three slow vortical modes and two fast gravity wave modes. These low-order models can be interpreted as describing the motions of a swinging spring [Lynch, 2002] or of a spring tied to a pendulum [Vanneste, 2006, 2008]. The small parameter equivalent to the Rossby number is the ratio of the (slow) pendulum to the (fast) spring oscillation frequencies. The fact that perturbative procedures lead, beyond the first orders, to divergent terms [Vautard and Legras, 1986; Warn and Ménard, 1986], as well as approaches involving numerical simulations [Lorenz and Krishnamurty, 1987; Camassa, 1995; Bokhove and Shepherd, 1996], and exponential asymptotics [Vanneste, 2004] have demonstrated the spontaneous generation of fast motions is inevitable (Figure 6). Vanneste [2004] has explicitly quantified the emission in this model as exponentially small in Rossby number, i.e., of a form involving $e^{-\alpha R_o}$, with a prefactor that involves algebraic powers of the Rossby number $R_o$. 
Figure 6. Evolution of \( y(t) \), one of the two fast variables of the Lorenz-Krishnamurty model, as calculated by Vanneste [2004], for Rossby numbers \( \epsilon = 0.15 \) (upper curve, offset by 0.02), \( \epsilon = 0.125 \) (middle curve, offset by 0.01), and \( \epsilon = 0.1 \) (lower curve). The balanced evolution of the flow leads to temporary variations of \( y \) near \( t = 0 \). For \( \epsilon = 0.15 \), conspicuous fast oscillations are excited and remain thereafter. This emission is very sensitive to \( \epsilon \) (exponential dependence).

A second line of evidence comes from mechanisms of spontaneous emission identified in full flows, i.e., described by a system of partial differential equations. The first is Lighthill radiation and constitutes an explicit example of spontaneous generation. Two other mechanisms of SAE are unbalanced instabilities (section 3.3) and transient generation in shear (section 3.4).

Lighthill radiation of gravity wave motions by balanced vortical motions [Ford, 1994a, 1994b, 1994c] is analogous to the radiation of acoustic waves by turbulent vortical motions described by Lighthill [1952]. The analogy is straightforward for the nonrotating shallow water equations which are equivalent to the two-dimensional equations for gas dynamics, with gravity waves replacing acoustic waves, and the Froude number \( F = U/\sqrt{gH} \), with \( g \) being gravity and \( H \) the layer depth, replacing the Mach number \( M = U/c_s \), where \( c_s \) is the speed of sound. The inclusion of rotation inhibits the emission of waves, as frequency matching between the vortical motion and the inertia-gravity waves only occurs for \( Ro > 1 \) [Ford, 1994a]. The smallness of \( F \) allows asymptotic investigation of the problem and has an essential implication regarding the scale of the waves: for the excited gravity waves having frequencies matching those of the balanced motion, of order \( U/L \), the dispersion relation for shallow water waves imposes that they have spatial scales \( \lambda \sim L/F \gg L \). Hence, there is a scale separation between the small balanced motion and the large-scale gravity waves that are emitted.

Figure 7. Illustration of Lighthill radiation, adapted from Ford [1994c]: (left) roll-up of the unstable potential vorticity strip as seen from the potential vorticity distribution and (right) radiation of gravity waves in the far-field, as seen from the time derivative of the surface height. Note the different vertical axes and the considerable scale separation between the two phenomena.
Many aspects of the emission can be summarized by rearranging the equations of motions in such a way as to obtain a wave equation on the left-hand side (lhs), forced by nonlinear terms on the right-hand side (rhs) [Ford, 1994c; Ford et al., 2000]:

$$\left( \frac{\partial^2}{\partial t^2} + f^2 - gh_0 \nabla^2 \right) \frac{\partial h}{\partial t} = \frac{\partial^2}{\partial x_i \partial x_j} T_{ij},$$

where $h$ is the height of the surface, $h_0$ is the height at rest, $f$ is the Coriolis parameter, and $T_{ij}$ result from the combination of the nonlinear terms of the equations. In itself, this rearrangement does not prove anything [Snyder et al., 1993; Plougonven et al., 2009]. When one adds assumptions on the regime parameter as above ($Ro > 1, F << 1$), one deals with Lighthill radiation: the waves are large scale, and the small-scale balanced motions are supposed to occur only in a compact region; hence, it is appropriate to consider that the waves are propagating on the background of a fluid at rest and that the forcing is a point, quadrupolar source. The quadrupolar nature of the forcing implies, in this setting, significant destructive interferences and hence weak emission (order $F^2$) [Ford et al., 2000].

As Ford et al. [2000, 2002] emphasized, one key feature of Lighthill radiation was that the emission is weak enough that the source can be described without taking the emission into account, e.g., from a balanced model. The lhs of (2) being the standard equation for gravity waves for a fluid at rest, standard intuitions apply: for example, Fourier transforms [Ford, 1994c] can be used to isolate the part of the rhs forcing that produces gravity waves (frequencies larger than $f$). Matched asymptotic expansions or Green’s functions can be used to solve the forced problem [Ford, 1994a, 1994b; Ford et al., 2000]. Gravity wave emission by balanced motions was investigated in rotating shallow water for unstable modes of axisymmetric vortices [Ford, 1994a], for the emission by an elliptic vortex [Ford, 1994b], for arbitrary localized balanced motions [Ford et al., 2000] and for the roll-up of an unstable shear layer [Ford, 1994c]. In the latter case, numerical simulations were used to describe the small-scale vortical motions, and knowledge of the resulting forcing, averaged in the streamwise direction, was successfully used to predict the large-scale inertia-gravity waves in the far field (see Figure 7).

The analysis of Lighthill radiation was extended to a continuously stratified fluid for the emission by an ellipsoidal vortex [Plougonven and Zeitlin, 2002]. The radiative instability of an axisymmetric vortex [Ford, 1994a] and the evolution of the elliptic vortex [Ford, 1994b; Plougonven and Zeitlin, 2002] can be interpreted as a coupling of Rossby waves on the potential vorticity (PV) gradient on the edge of the vortex [Brunet and Montgomery, 2002] with inertia-gravity waves in the far-field. The amplitudes of the emitted waves are found to scale as $F^2$, and hence the back-reaction on the vortical motions only occurs on very slow timescales ($F^{-4} T$), where $T$ is the advective timescale of the balanced motion.

Rankine vortices were used for the above studies, for analytical tractability. In more realistic cases, the PV of the vortices likely have a continuous transition from the intense values in the vortex core to the null values in the far-field. In this case, mixing at a critical level, where the PV gradient is weak but nonzero, may inhibit the growth of these radiative instabilities [Schecter and Montgomery, 2006]. The regime of parameters for Lighthill radiation make it relevant for strong supercell mesocyclones and hurricanes [Schecter (2008) and ref. therein].

The study of Lighthill radiation was recently extended with numerical experiments to carry out a systematic parameter sweep [Sugimoto et al., 2008], and also to spherical geometry [Sugimoto and Ishii, 2012]. The emission of gravity waves in a 2-layer shallow water model, on the $\beta$-plane, was recently revisited with an emphasis on very high resolution [Wirth, 2013]. These simulations confirm the presence of a weak, continuous emission of gravity waves (without any sudden bursts of emission).

### 3.3. Unbalanced Instabilities

The stability analyses of midlatitude synoptic flows focus on basic flows that are balanced, such as sheared zonal flows in geostrophic balance [e.g., Vallis, 2006]. The main modes of instability have been discovered and discussed in balanced models such as the quasi-geostrophic approximation [e.g., Eady, 1949]. Such instabilities can therefore be called balanced instabilities. In contrast, unbalanced instabilities are filtered out in all balanced models [Vanneste, 2013], because they involve some form of unbalanced motions, typically gravity waves. An unbalanced instability growing in a balanced flow can hence produce a growing gravity wave component to the flow, and as such constitutes a mechanism for spontaneous generation.
One motivation for the study of these various unbalanced instabilities has come from the need to understand, in the ocean, the energy transfer from balanced, large-scale flow down to scales where energy is dissipated (see [McWilliams et al., 2001] and section 6.4). Another motivation has been to better understand the dynamics of two-layer systems encountered in laboratory experiments (see section 5.1).

A flow for which unbalanced instabilities have received considerable attention is a constant vertical shear above a flat surface. The classical baroclinic instability can be obtained in the quasi-geostrophic approximation for such a shear between a flat surface and a rigid lid [Eady, 1949]. Stone [1970] and Tokioka [1970] independently extended the stability analysis to the linearized primitive equations and obtained unbalanced modes of instability beyond the Eady cutoff. The spatial structure of these modes was elucidated by Nakamura [1988]; he showed that the modes changed character through the inertial-critical level (ICL), where the Doppler-shifted wave period is equal to the inertial period. The stability analysis was extended to nonzero meridional wave number \( l \) by Yamazaki and Peltier [2001a, 2001b]. The growth rates of these normal modes [Molemaker et al., 2005] and the spatial structure [Plougonven et al., 2005] were both revisited recently. The unstable modes consist of an Eady edge wave [Gill, 1982] between the ground and the ICL, and sheared gravity waves above (see Figure 8). A WKBJ approximation gives an accurate description of the normal mode, including its exponentially small growth rate (Vanneste, unpublished work, 2012).

Unbalanced instabilities can involve different types of waves, from IGW [e.g., Plougonven et al., 2005] to Kelvin waves [e.g., Kushner et al., 1998], and have been identified in different flows: two layer sheared flow [Sakai, 1989], sheared flow over a slope [Sutyrin, 2007, 2008], horizontal shear [Vanneste and Yavneh, 2007], stratified Taylor-Couette flow [Yavneh et al., 2001; Molemaker et al., 2001], vortices [LeDizès and Billant, 2009], a front of potential vorticity [Dritschel and Vanneste, 2006], and elliptical instability [McWilliams and Yavneh, 1998; Aspden and Vanneste, 2009].

The main message is that unbalanced instabilities illustrate how balanced motions and gravity waves couple spatially in a background flow. Whereas for small perturbations to a fluid at rest there is a clear-cut distinction between balanced motions and gravity waves [e.g., Reznik et al., 2001], in a nontrivial flow such as a shear the separation between balanced motions and gravity waves is no longer clear [Plougonven et al., 2005]. Consider for example a constant, unbounded shear above a flat surface, with an initial perturbation in the form of an Eady edge wave. An Eady edge wave is a neutral solution in the quasi-geostrophic approximation, and an archetype of balanced motions. In the linearized primitive equations, it will project on unstable modes of which it constitutes the lower part, the upper part consisting in sheared gravity waves.

The unstable character of such modes may not be so important because unbalanced modes generally have small growth rates relative to balanced instabilities present in the same flows [Stone, 1970; Molemaker et al., 2005]. In addition, there are indications that they saturate at weak amplitudes, as suggested by the numerical simulations of Gula et al. [2009a] who revisited instabilities coupling a Rossby wave and a Kelvin wave in a channel. Recently, careful laboratory experiments (see section 5.1) have provided the first evi-
evidence of these instabilities in real flows, and confirmed the weakness of their growth. The stability study of realistic (continuous) frontal states [Snyder, 1995] also provides evidence for the weakness of unbalanced instabilities.

### 3.4. Transient Generation by Sheared Disturbances

The evolution of potential vorticity anomalies in a sheared flow [Vanneste and Yavneh, 2004] leads to a transient generation of gravity waves. This differs from the unbalanced instabilities described above in several respects: 1) the generation of gravity waves occurs at a specific time, and 2) the final amplitude of the waves can be predicted within the linear theory [Vanneste, 2008]. Vanneste and Yavneh [2004] quantified the emission of gravity waves for a sheared disturbance at one along-shear wave number, and demonstrated that the final amplitude of the waves is proportional to

\[ \varepsilon^{-1/2} \exp\left(-\frac{\alpha}{\varepsilon}\right), \]

where \( \varepsilon \ll 1 \) is the Rossby number and \( \alpha \) is a constant. As for the spontaneous generation in the Lorenz-Krishnamurty model [Vanneste, 2004], exponential asymptotics were necessary to calculate this exponentially weak emission. The solutions obtained for one wave number can be combined to describe the emission by small-amplitude localized features of the flow such as a sheared vortex [Olafsdottir et al., 2008]. At initial time, the PV anomaly tilts against the shear, and gravity waves are absent. Near the time when the tilt changes sign, gravity waves are emitted. The same phenomenology is found for the transient emission of waves from vertically sheared PV anomalies [Lott et al., 2010, 2012a] (see Figures 5 of Lott et al. [2010] and 7 of Lott et al. [2012a]). Hence, these latter studies can be seen, regarding the phenomenon described, as counterparts of Olafsdottir et al. [2008] for a vertical shear.

In contrast to Vanneste [2004], the transient emission in a vertical shear was described by Lott et al. [2010] using a modal (Fourier) decomposition, with each component describing the motions associated to a PV distribution with sinusoidal dependencies in the horizontal, and a Dirac-\( \delta \) in the vertical. Hence, regarding the mathematical approach, these studies can also be seen as a counterpart of Plougonven et al. [2005] without a surface: the equation that is solved for the vertical structure of the modes is the same, but with different boundary conditions.

The relationships between the different approaches (modal versus nonmodal) in a vertical shear are discussed by Mamatsashvili et al. [2010]. This highlights the connections between the different mechanisms of spontaneous emission. Both unbalanced instabilities and transient emission fundamentally rely on shear (on Doppler-shifting) to connect motions that have different intrinsic timescales.

The transient emission of gravity waves by sheared regions has been investigated also in different contexts, to determine what gravity wave response could be expected from a stochastically perturbed shear layer or jet [Lott, 1997; Bakas and Farrell, 2008, 2009a, 2009b]. Investigation of momentum transport by gravity waves in a stochastically forced jet has shown for instance that the jet not only passively filters waves, but also amplifies portions of the spectrum, leading to possibly significant decelerations of the jet [Bakas and Farrell, 2008].

### 3.5. Shear Instability

Another possible route for the excitation of GWs from jets and fronts involves shear instabilities on small scales. Shear instabilities are here treated separately from the other unbalanced instabilities because they occur at large Rossby numbers, such that the background rotation is not relevant for their development. In the course of frontogenesis, both near the surface and at upper-levels, very intense shear layers are produced, potentially leading to shear instability [e.g., Snyder, 1995; Esler and Polvani, 2004]. As such, this constitutes a mechanism for spontaneous emission; however, the scales of shear instability are short enough that it has generally been considered in nonrotating flow, and hence is not discussed in the literature on spontaneous emission.

Over the past four decades, several candidate mechanisms have been investigated by which shear instabilities excite gravity waves, in a direct or indirect way, in a linear or nonlinear framework. One essential difficulty here lies in the range of scales involved, from tens of meters for the turbulence initiated by the
instability of a shear layer to thousands of kilometers for the baroclinic instability setting the environmental shear and modulating the background stratification.

The first investigations of possible mechanisms focused on the linear stability analysis of an atmospheric shear layer. The aim was to determine whether unstable modes exist that comprise a radiating GW above the shear layer or a jet [Lalas and Einaudi, 1976; Lalas et al., 1976; Mastrantonio et al., 1976]. Although such unstable modes do exist, their growth rates are always considerably smaller than those of KH instability [Fritts, 1980]. The latter always occurs on small scales such that their signature above and below the shear layer is evanescent. McIntyre and Weissman [1978] point out a fundamental difficulty for shear instabilities to generate gravity waves: to couple with propagating gravity waves above the shear layer, it is necessary that the (real part of the) phase speed, \( c \), and the horizontal wavenumber, \( k \), meet the phase speed condition:

\[
U - N/k < c < U + N/k,
\]

where \( U \) is the wind velocity, \( N \) is the Brunt-Väisälä frequency. For large values of \( k \), the interval becomes very narrow and only evanescent responses are found in the layer above the shear. Hence, generation from shear instabilities likely involves nonlinear mechanisms.

The first nonlinear mechanism to be investigated as a route to larger scales was vortex pairing [Davis and Peltier, 1979]. To obtain significantly larger scales, Fritts [1982, 1984] and Chimonas and Grant [1984] described the interaction of two KH modes having nearby wavenumbers, \( k \) and \( k + \delta k \). These weak nonlinear interactions produce scales \( 2\pi/\delta k \), large enough to radiate gravity waves. This mechanism, called envelope radiation, has been further investigated by Scinocca and Ford [2000] using direct numerical simulations of the 2-D evolution of a region of unstable shear. They focused on the early stages of the instability (when the two-dimensionality is relevant) and on quantifying the momentum fluxes associated with envelope radiation. Going beyond the two-dimensional approximation Tse et al. [2003] simulated the three-dimensional turbulence in a forced, unstable jet. In a subsequent study, Mahalov et al. [2007] focused on the emission of gravity waves and confirmed their capacity to exert a significant drag on the flow emitting them.

The end effect of the shear instability will be to mix the fluid over the region where it developed. This mixing occurs over a short timescale relative to the inertial period, so the fluid is forced out of balance and will then undergo geostrophic adjustment to recover a balanced state, and emit inertia-gravity waves in the process [Bühler et al., 1999]. Bühler and McIntyre [1999] calculated the subsequent propagation of the emitted waves in a mean wind profile representative of the summer stratosphere. They concluded that the contribution of this source could not safely be neglected in the global angular momentum budget.

The above studies focused on shear layers in a fluid having constant Brunt-Väisälä frequency. Another possibility consists in having variations of the stratification leading to either propagating wave instabilities [Lott et al., 1992; Sutherland, 2006] or to a coupling of the shear instability to upward propagating waves [Sutherland et al., 1994; Sutherland and Peltier, 1995]. This may be relevant as the upper-tropospheric jet-stream is indeed just below the tropopause and its sharp jump in stratification [Birner et al., 2002; Gettelman et al., 2011].

In summary, theoretical and numerical studies support the notion that gravity waves generated from shear instabilities need to be considered for middle atmospheric dynamics, but the complexity of the flows considered has hindered theoretical progress in quantifying them, while their small scales have made observations difficult.

4. Propagation and Maintenance

The framework of parameterizations and the resulting demand for a specific description of sources encourages one to think separately of the gravity wave sources and of their subsequent propagation (in a vertical column for parameterizations). Now, several mechanisms described above (unbalanced instabilities and transient generation, sections 3.3 and 3.4), precisely emphasize the key role played by a varying background wind for the appearance of the waves. In more complex flows (sections 2.2 and 5), studies of wave emission emphasize the importance of propagation effects. This motivates a pause in the review of generation mechanisms to briefly describe wave ducting, ray tracing, and wave capture.

4.1. Ducted Gravity Waves

Ducting of gravity waves between the ground and a layer acting as a partial reflector has been modeled by Lindzen and Tung [1976]. It occurs when a stable layer is present near the ground, capped by a layer which efficiently reflects waves (e.g., of low stability, or conditionally unstable, possibly beneath a critical level). The stable layer needs to be thick enough, and not to contain a critical level. Ducted waves, reflecting off the
ground and (partially) at the top of the layer, may travel significant distances in the horizontal, with energy leaking only slowly through the top of the duct. In consequence, such almost free waves [Lindzen and Tung, 1976] need only a weak forcing to be present, and the geometry and stability of the duct selects some of their characteristics. One characteristic selected by the duct is the phase speed

$$C_D \sim \frac{N_D H}{\pi \left( \frac{1}{2} + n \right)}, \quad n = 0, 1, 2, \ldots$$

where $N_D$ is the Brunt-Väisälä frequency in the duct, and $H$ its height. The tallest wave ($n = 0$) will be least damped, and is hence of greatest interest. This is a clear example of how the environment in which gravity waves are forced selects certain characteristics of the waves, making it in practice more important to know the duct rather than the details of the forcing.

The relevance of ducting has been shown by numerous case studies focusing on lower tropospheric waves in the vicinity of surface fronts [e.g., Eom, 1975; Bluestein and Jairn, 1985; Parsons and Hobbs, 1983; Uccellini and Koch, 1987; Nicholls et al., 1991; Powers and Reed, 1993; Zhang and Koch, 2000; Zhang et al., 2003; Knippertz et al., 2010]. Ducted gravity waves are found propagating ahead of cold fronts, and on smaller scales ahead of gust fronts [Knupp, 2006], and can play a significant role in triggering convection. The complex interaction between ducted gravity waves and moist convection that maintains and amplifies the mesoscale waves is also referred to as ducted wave-CISK model [Powers, 1997; Zhang et al., 2001]. Other mechanisms leading to maintenance of gravity waves, e.g., solitary wave dynamics [Lin and Goff, 1988], lie beyond the scope of the present paper and will not be discussed.

### 4.2. Ray Tracing

A common approach to investigate the propagation of gravity waves in complex flows has been the use of ray tracing, which we briefly recall below (see Lighthill [1978] or Bühler [2009] for a complete discussion, and Aspden and Vanneste [2010] for an alternative derivation). It has typically been used in case studies to identify the origin of observed waves [Guest et al., 2000; Hertzog et al., 2001], and in idealized simulations to identify sources and follow emitted waves [Lin and Zhang, 2008; Wang and Zhang, 2010]. Many of these studies use the ray tracing software package developed in Eckermann and Marks [1996, 1997] with various complex background flows.

Consider a wave-packet described by

$$u(x, t) = A(x, t) e^{i\theta(x, t)}$$

for the $x$-component of the velocity, with $A$ a slowly changing amplitude and $\theta$ a fast-varying phase. The local wave vector and frequency are defined by $k(x, t) = \nabla \theta$ and $\omega(x, t) = -\theta_t$, where the subscript is used to denote partial derivation. They vary slowly (as $A$ and the background flow), and are assumed to locally satisfy the dispersion relation:

$$\omega = \Omega(k(x, t), x, t) = \hat{\Omega} + Uk,$$  

with $\omega$ the absolute frequency and $\hat{\Omega}(k, x, t)$ the appropriate dispersion relation.

Now, cross-differentiating the definitions of $k$ and $\omega$ we can obtain $k_t + \nabla \omega = 0$. Substitution into (5), using the chain rule and the fact that $\nabla \times k = 0$ yields:

$$\frac{dx}{dt} = \frac{\partial \Omega}{\partial k} \quad \text{and} \quad \frac{dk}{dt} = -\frac{\partial \Omega}{\partial x}$$

where

$$\frac{d}{dt} = \frac{\partial}{\partial t} + (U + \hat{\mathbf{c}}_g) \cdot \nabla \quad \text{and} \quad \hat{\mathbf{c}}_g = \frac{\partial \hat{\Omega}}{\partial k}.$$

is the group velocity. An additional equation, generally for the conservation of wave action $A = E/\hat{\omega}$, with $E$ the energy of the wave, is necessary to follow the evolution of the amplitude of the wave-packet [Bühler, 2009].
4.3. Wave Capture
Ray tracing allows the investigation, with simple considerations, of how the flow in a jet exit region may have a specific effect on inertia-gravity waves. In studies that have emphasized jet exit regions as particularly favorable to the occurrence of large-amplitude gravity waves, it has often been assumed, implicitly, that waves were large because they were generated there. This overlooks another possibility of interest: that jet exit regions have a particular significance not only for the generation, but also for the propagation of gravity waves.

Case studies have highlighted a specific region within the jet, where the flow decelerates and the streamlines are diffuent. The effect of such a background flow on wave packets propagating through them has been emphasized in theoretical studies as wave-capture [Badulin and Shira, 1993; Bühler and McIntyre, 2005]. The combination of strong deformation and vertical shear can lead to the contraction of the wave packet to smaller and smaller scales, until dissipation occurs, without having the intrinsic frequency tending to either bound of the GW frequency spectrum.

Quantifying this effect introduces new possible interactions between waves and mean flows [Bühler and McIntyre, 2003, 2005], but requires to take into consideration horizontal variations of the background flow, i.e., to consider propagation in $U(x, y, z)$. This is in contrast to the columnar approximation made for parameterizations (where only $U(z)$ is considered), and which is encouraged by parallel computing.

The dispersion relation for waves in a stratified fluid differs crucially from that in shallow water: in the latter, short-scale waves necessarily have large frequencies and fast group velocities (recall $\omega^2 = f^2 + gH(k^2 + \beta^2)$). In the former, the group velocity of a small-scale wave packet is small, e.g. Gill [1982]. This warrants an analogy [Bühler, 2009] between the evolution equation for the wave vector and for the evolution of the gradient of a passive, conserved tracer $\phi$, respectively:

$$\frac{dk}{dt} = - (\nabla U) \cdot k \quad \text{and} \quad \frac{D \nabla \phi}{Dt} = - (\nabla U) \cdot \nabla \phi,$$

(7)

where the first equation may be written with indicial notation as $dk_i/dt = -\partial_U / \partial x_i k_i$. Importantly, the two equations differ in their operators on the lhs by

$$\frac{d}{dt} - \frac{D}{Dt} = \hat{c}_g \cdot \nabla.$$

Now, assuming the background flow to be layerwise nondivergent, $U = (U, V, 0)$, with $U_x + V_y = 0$, the evolution of the advected tracer gradient is governed by the sign of

$$D = -U_x V_y + V_x U_y = \frac{1}{4} \left( (U_x - V_y)^2 + (V_x + U_y)^2 - (V_x - U_y)^2 \right).$$

(8)

The first two terms on the rhs of (8) constitute the strain [Batchelor, 1967], and the last is the vertical component of the relative vorticity. $D$ is also referred to as the Okubo-Weiss parameter and extensively discussed in studies of tracer advection (e.g., Lapeyre et al., 1999) and references therein.

If the wave packet remains where the strain dominates ($D > 0$), the wave number experiences exponential growth (see Bühler [2009], section 14.3). As a simple example, consider a pure deformation flow with extension along the $y$-axis, with vertical shear: $U = -ax + \beta z$ and $V = ay + \gamma z$. Equation (7) then yields $k = k_0 e^{\omega t}$, $l = l_0 e^{-at}$ and $m = -a^{-1} \beta k(t)$ as $t \to +\infty$. Asymptotically, the wave vector will tend to

$$(k, l, m) \to k_0 e^{at} \left( 1, 0, \frac{U_z}{U_x} \right),$$

for $t \to \infty$, and with $k_0$ the initial value of wave number $k$. Now, the above considers the action of only one region of strain on a wave packet. As a packet moves within the flow (by advection and by its own propagation), it may encounter different regions of strain, and Aspden and Vanneste [2010] show that this will lead to growth of the wave number. Haynes and Anglade [1997] describe the effect of this process for tracer gradients.

We emphasize two implications: first, for wave packets that have a long enough residence time in jet exit regions, where deformation and shear are large, propagation effects will favor certain orientation and intrinsic frequency, and contraction of the wavelength. Second, this is only an asymptotic result, neglecting
spatial variations of the background shear and strain. Its efficiency will depend on the residence time of the wave packet in the jet exit region, with little sensitivity to the initial condition. This effect has been named wave-capture, because the asymptotic calculation suggests contraction of the wavelength down to dissipation. In practice, it may be that capture is only partially realized, but this effect will nonetheless constrain wave characteristics, and the term wave-capture will be used to designate this influence.

5. Generation Mechanisms: Laboratory and Modeling Experiments

There is a certain discrepancy between the simplicity necessary for analytical studies, e.g., plane-parallel unbounded shear-flows (sections 3.3-3.4), and the complex, three-dimensional flow patterns highlighted in observations, e.g., jet exit regions (section 2.2). Laboratory experiments (section 5.1) and idealized simulations (sections 5.2-5.4) have provided a realm for exploring spontaneous emission in flows of intermediate complexity, bridging the two, and establishing a convincing sketch of the generation mechanism involved near jet exit regions.

5.1. Laboratory Experiments

Laboratory experiments provide valuable examples of real flows, in which a fundamental dynamical mechanism may be identified, and to some extent isolated. Understanding these experiments can greatly enhance our understanding of the atmosphere and ocean, provided the mechanisms at play are the same.

Several experiments have been reported as exhibiting spontaneous generation of gravity waves in stratified fluids, in particular in a rotating annulus forced either by the thermal gradient between the inner and outer cylinder, or by shear between the bottom and top lid.

A classical laboratory experiment of baroclinic instability has focused on a shear-driven fluid in a rotating annulus [Hart, 1972]. In such a configuration, with an aspect ratio of 2 (height / width) for each layer, Lovegrove et al. [2000] and Williams et al. [2005] used detailed measurements of the height of the interface between two immiscible fluids to investigate the emission of gravity waves. In a regime dominated by large scale baroclinic waves (wave number 2), small-scale features (wave number between 30 and 40, [Williams et al., 2008]) occur which are interpreted as inertia-gravity waves. Their amplitude is estimated to vary linearly with Rossby number in the range 0.05 < $Ro$ < 0.14 [Williams et al., 2008]. The generation mechanism was argued by Williams et al. [2005] to be Lighthill radiation, because the forcing terms (as in equation (2) and assuming shallow water [Ford et al., 2000]) are colocated with the gravity waves. However, the flow regime ($Ro \ll 1$, and not shallow water) and the scale separation (small-scale waves) differ completely from those for Lighthill radiation, and the amplitude varies linearly although the hypothesized forcing is quadratic. Hence one may say that the generation mechanism is not yet adequately explained.

A similar experiment has recently been carried out by Scolan et al. [2011] but with a salt stratification including a sharp transition rather than immiscible fluids and with an aspect ratio ($\sim$ 0.2) compatible with a shallow water interpretation. Interpretation is supported by the complete stability analysis for two-layer shallow water shear layers flows in an annulus obtained by Gula et al. [2009b], which includes an unbalanced instability (Rossby-Kelvin, see section 3.3). Scolan et al. [2011] identify this unbalanced instability, for the first time in laboratory experiments. They also find that small-scale perturbations are present in many regimes of parameters. These small-scale features are argued in many cases to result from Hölmböe instability [e.g., Lawrence et al., 1991]. This instability occurs when a sharp density interface is colocated with a thicker shear layer and is hence particularly relevant for the experiments with immiscible fluids of Williams et al. [2005].

Thermally driven annulus experiments have also reported small-scale features [Read, 1992] which could be gravity waves. Numerical simulations have proved necessary to confirm this [Jacoby et al., 2011] and have further identified an instability of the lateral boundary layer as the generation mechanism. Its location in azimuth remains unexplained but is likely tied to the separation of the large-scale geostrophic jet from the inner boundary. Randriamampianina [2013] proposes an alternate explanation, also involving interaction with the inner boundary. This example and the reinterpretation of the waves investigated by Williams et al. [2005] as Hölmböe instability [Scolan et al., 2011] emphasize the importance of boundary or interfacial layers in such laboratory experiments, making it more difficult to relate these results to atmospheric or oceanic flows.

Another unbalanced instability has been identified in laboratory experiments: Riedinger et al. [2010a] have analyzed the radiative instabilities of axisymmetric, columnar vortices in nonrotating, stratified fluid. The
radiative instability of the flow around a rotating cylinder has been described theoretically and very clearly displayed in experiments [Riedinger et al., 2011]. The robust agreement between theory and experiments in this somewhat contrived configuration makes the (difficult) experimental identification of the radiative instability of a columnar vortex all the more convincing [Riedinger et al., 2010b]. Remarkably, this is the first laboratory evidence of an unbalanced, radiative instability.

Spontaneous emission was also investigated during the collision and rearrangement of two dipoles in the interior of a two-layer fluid [Afanasyev, 2003]. The experiments confirmed the radiation of interfacial gravity waves, occurring when fluid parcels underwent strong accelerations, such that the spatial scale and the Lagrangian timescale matched the dispersion relation.

Perhaps the clearest experimental evidence of spontaneous emission was provided by the study of an unstable coastal jet in a two-layer fluid [Afanasyev et al., 2008]. A clever visualization technique (Altimetric Imaging Velocimetry) [Rhines et al., 2006] allowed the detection and precise quantification of the waves emitted and a description of the vortical flow emitting the waves at very high resolution. A notable difference relative to other studies on spontaneous generation is that the emitted waves are inertial waves in the unstratified lower layer, hence not constrained by \( \omega \geq f \). Waves were radiated away from the meanders of the baroclinic instability when the deformation radius was short enough that the characteristics of the meanders matched the dispersion relationship for the inertial waves (see Figure 9). In experiments with larger deformation radius, single events of emission could be isolated, emphasizing regions of strong curvature and large flow accelerations. Emitted waves represented only a small fraction, about 0.5\%, of the total energy of the flow.

5.2. Early Simulations

Due to limited computational resources, early simulations focused on shallow water systems (one or two layers) or on two-dimensional frontogenesis. The numerical study, in a two-layer model, of the geostrophic adjustment of a jet streak by Van Tuyl and Young [1982] deserves to be highlighted because they identified several essential issues which, although simple, have sometimes been overlooked thereafter. They simulated the adjustment of perturbations added to a jet streak and emphasize how the background flow crucially changes the adjustment and the wave dynamics. They give three reasons why traditional approaches (more specifically, normal mode techniques of [Machenhauer, 1977; Baer and Tribbia, 1977]) fail to separate gravity waves and balanced motions in the vicinity of jet streaks: “1) the gravity-inertia modes are eigenfunctions for a base state of rest, rather than a sheared, time-dependent jet; 2) the methods may not work for strong accelerations (Rossby number of order unity (…)); and 3) the frequency separation has been based upon Eulerian (fixed frame) frequencies, rather than Lagrangian (Doppler-shifted) ones” [Van Tuyl and Young, 1982, p 2039]. Indeed, points 1 and 3 underlie the spontaneous generation of gravity waves in a shear (sections 3.3 and 3.4), and point 2 (\( Ro \geq 1 \)) is a starting point for Lighthill radiation.

The simulations of Van Tuyl and Young [1982] may be regarded as early prototypes of the recent dipole experiments (section 5.4). With anticipation, they suggest that gravity wave modes near jet streaks, although usually discarded as meteorological noise, “may eventually show their more persistent members to be a
complex part of the jet streak signal” (p 2038). Other simulations with the one- or two-layer shallow water model have been carried out to investigate the spontaneous emission of gravity waves and have been described in section 3.2.

Early numerical experiments of spontaneous generation described two-dimensional frontogenesesis. Indeed, major features of frontogenesesis can be understood in a two-dimensional framework [Hoskins, 1982], which greatly simplifies the problem and made it possible to attain higher resolutions. Although frontogenesesis can in some instances be considered as an adjustment [e.g., Kalashnik, 1998, 2000], it is a specific process, central to midlatitude dynamics and deserves its own discussion, distinct from that of geostrophic adjustment (section 3.1).

A first study of gravity waves emitted by fronts was carried out with a mostly analytical approach by Ley and Peltier [1978]. They calculated the far-field gravity wave response to a frontogenesis event modeled by semigeostrophy, assuming the background to be at rest when calculating the gravity wave response. Subsequent studies explicitly simulated the frontal collapse with different numerical methods [Gall et al., 1987, 1988], including a Lagrangian description [Garner, 1989], but Snyder et al. [1993] showed that part of the gravity waves discussed were spurious, due to poor initialization and an inconsistency between the aspect ratios of the grid (Δz/Δx) and of the frontal slope [Lindzen and Fox-Rabinowitz, 1989]. Snyder et al. [1993] simulated both inviscid frontogenesis prior to frontal collapse and postcollapse frontogenesis with horizontal diffusion, with frontogenesis forced by either deformation or shear. Emission occurred when the advective timescale, which decreases as frontogenesis proceeds and the cross-frontal scale shrinks, became comparable to or shorter than the inertial period. Waves were most prominent in the postcollapse solutions, above the surface front. This emission was explained as the linear response, in the frontogenetical background flow, to the cross-front accelerations neglected by semigeostrophy.

More realistic simulations focusing on gravity wave generation were carried out by Griffiths and Reeder [1996], who considered a domain including a stratosphere. The three cases of deformation frontogenesis that were simulated all showed emission of large-scale, low-frequency waves from the upper level front and propagation up into the stratosphere. Their comparison revealed that a determining factor for the amplitude of the emitted waves was the rapidity of the frontogenesis rather than its intensity (estimated by the maximum cyclonic vorticity). Reeder and Griffiths [1996] used ray tracing to confirm the origin of the waves from the upper level front and its initial near-inertial frequency (\(\hat{\omega} \sim 1.3f\)). The emission was successfully interpreted, with reference to Lighthill radiation [Ford, 1994c], as the linear response to the nonlinear terms from the frontal circulation. The waves reproduced by linear simulations were not very sensitive to the definition of the forcing (defined from the full simulation or only its balanced approximation), but their characteristics were strongly influenced by the background flow. Indeed, note that the equations are linearized around a background flow consisting of the imposed deformation and transverse shear not around a state of rest. This profoundly modifies the problem relative to Lighthill radiation (see section 5.4).

5.3. Idealized Baroclinic Life Cycles

Idealized life cycles of baroclinic instability provide more realistic flows to investigate spontaneous emission, but requires significant computational resources as an additional spatial dimension is needed. O’Sullivan and Dunkerton [1995] simulated a baroclinic life cycle on the sphere (wave number 6, following Simmons and Hoskins [1978]) with a spectral truncation at wave number 126 (T126, approximately equivalent to a horizontal grid spacing of 1°). Inertia-gravity waves with intrinsic frequencies between \(f\) and \(2f\) during the nonlinear stage of the development of the baroclinic wave, principally in the jet-stream exit region in the upper troposphere (see Figure 10). Surface fronts were shown not to be the source of these waves. They subsequently propagated horizontally within the jet, but only few IGWs penetrated the lower stratosphere. O’Sullivan and Dunkerton [1995] showed maps of the Lagrangian Rossby number with a large-scale maximum roughly coincident with the waves and put forward geostrophic adjustment as the generation mechanism.

The simulations and interpretations of O’Sullivan and Dunkerton [1995] have become a milestone for several reasons: they explicitly showed IGWs generated by jets, with more realism than 2-D frontogenesis simulations, allowing essential features emphasized from observations (low frequency, jet exit region) to be reproduced. As a consequence, their interpretation in terms of geostrophic adjustment and the
Figure 10. (a) Geopotential height and wind at 503 hPa, at day 10 of the idealized baroclinic life cycle of O'Sullivan and Dunkerton [1995] and (b) divergence of the horizontal wind at 130 hPa at the same time. Contour interval is $10^{-3}$ s$^{-1}$, with thick contours for positive values, and thin contours for negative values. Adapted from O'Sullivan and Dunkerton [1995].

confirmation of the relevance of the Lagrangian Rossby number as a diagnostic have guided interpretations in subsequent studies, in particular for observations [e.g., Pavelin et al., 2001; Plougonven et al., 2003].

As shown by sensitivity tests, the simulations of O'Sullivan and Dunkerton [1995] did not converge numerically (see their Figure 9), which was somewhat controversial at the time. In fact, a contemporaneous study by Bush et al. [1995] used very similar idealized baroclinic life cycles (with $\Delta x \sim 60$ km) to analyze the degree of balance of the flow. However, the analysis of the emitted waves strongly suggested that these were a numerical artifact, again due to the shallow slope of the front near the surface [Lindzen and Fox-Rabinowitz, 1989]. These numerical issues raise two questions: (1) At what resolution would the gravity waves converge, and what small-scale gravity waves would then be obtained? (2) How should one interpret such gravity waves from simulations that have not converged?

Regarding the first question, the resolution used by O'Sullivan and Dunkerton [1995] only allowed subsynoptic scale inertia-gravity waves with horizontal wavelengths of 600–1000 km to be described. Consequently, Zhang [2004] performed multiply nested mesoscale numerical simulations with horizontal resolution down to 3.3 km to study the generation of mesoscale gravity waves during the life cycle of idealized baroclinic jet-front systems. Long-lived vertically propagating mesoscale gravity waves with horizontal wavelengths ~100–200 km are simulated originating from the exit region of the upper tropospheric jet streak, in a manner consistent with past observational studies (see Figure 11). The residual of the nonlinear balance equation is found to be a useful index in diagnosing flow imbalance and predicting the location of wave
Figure 11. Pressure and divergence of horizontal wind, at $z = 13$ km, in the baroclinic life cycle simulated by Zhang [2004]. Distance between the tick marks is 300 km. Contours for divergence are every $0.21\times10^{-5}$ s$^{-1}$.

generation. Zhang [2004] proposed the term balanced adjustment to describe the continuous radiation of waves within the developing baroclinic wave (see section 3.1).

To further investigate the sources and propagation of gravity waves in the baroclinic jet-front systems, Lin and Zhang [2008] carried out ray tracing from the four groups of waves they identified in the lower stratosphere, with horizontal wavelengths ranging from 100 to 350 km. It was thus shown that both the upper tropospheric jet-front system and the surface front contribute as sources of waves and that the background flow strongly influenced the characteristics of the waves during their propagation.

Wang and Zhang [2007] investigated the sensitivity of mesoscale gravity waves to the baroclinicity of the background jet-front systems by simulating different life cycles of baroclinic waves. Vertically propagating mesoscale gravity waves were systematically found in the exit region of upper tropospheric jet streaks. The intrinsic frequencies of these gravity waves were found to increase with the growth rate of the baroclinic waves showing a strong sensitivity to the timescale of the evolution of the balanced flow as in Reeder and Griffiths [1996].

Regarding the second question, Plougonven and Snyder [2005] have shown that simulations that did not converge numerically nevertheless could carry relevant information regarding the location, the horizontal orientation and the intrinsic frequency $\hat{\omega}$ of the waves in jet exit regions. The reason is that those characteristics are largely determined by propagation through the large-scale flow (see section 4.3), which influences orientation and intrinsic frequency $\hat{\omega}$. The large-scale strain causes a wave packet’s wave number to increase exponentially along a ray, so that details of the waves will always be sensitive to resolution. Evidence for this effect also comes from comparison of simulated waves with observations [Plougonven and Teitelbaum, 2003] and from the insensitivity to resolution of $\hat{\omega}$ for waves in jet exit regions [Plougonven and Snyder, 2007].

Now, the above studies emphasized gravity waves emanating from the upper level jet, not surface fronts, but they only explored one type of baroclinic life cycle development. In order to test the sensitivity of the wave generation to the background flow, Plougonven and Snyder [2007] ran two very different baroclinic life cycles, one with cyclonic development and the other with an anticyclonic development [Thorncroft et al., 1993]. In the cyclonic run, gravity waves were found in the jet exit region that are clearly emitted by the jet (both upward and downward wave packets are found), and the waves have subsynoptic scale, similar to those described by O’Sullivan and Dunkerton [1995]. In the anticyclonic run, the most conspicuous waves are found ahead of the surface cold front (see Figure 12), reminiscent of those found in 2-D frontogenesis studies, and have a different sensitivity to resolution: as resolution increases, their vertical wavelength remains unchanged while the horizontal one decreases, yielding higher frequencies (up to $3f$): these waves
are not undergoing wave capture. Their generation seems tied to an obstacle effect (strong surface winds impinging on the cold front), as in the case study of Ralph et al. [1999].

Baroclinic life cycles in a very different configuration (triply periodic domain, initial jet specified by strong interior PV anomalies) have been carried out by Viúdez and Dritschel [2006] to study spontaneous emission with a sophisticated code and inversion for the balanced flow. Waves with intrinsic frequencies close to inertial \( (N/f ∼ m/k) \) were produced in very localized bursts where the flow has strong curvature, on the anticyclonic side of the jet. One packet remains trapped within the vortices, while another propagates significantly outward.

Waite and Snyder [2009] carried out baroclinic life cycle experiments at high resolution \( (Δx = 10 \text{ km}, Δz = 60 \text{ m}) \), which revealed three types of waves spontaneously generated (reminiscent of Snyder et al. [1993], Zhang [2004], and Plougonven and Snyder [2007] respectively). At later times, these localized packets give way to more disordered wave signatures filling the whole region of the baroclinic jet and vortices.

5.4. Dipoles

Both observations and idealized baroclinic life cycles have stressed jet exit regions as favored sites for the appearance of conspicuous inertia-gravity waves. Now, a simple model of a jet exit region is provided by a dipole vortex made of a cyclone and an anticyclone propagating together as a coherent structure [e.g., Cunningham and Keyser, 2000]. Numerical simulations of dipoles on an \( f \)-plane have been carried out by several different groups, using very different models and different initial conditions: Snyder et al. [2007] started from an exact quasi-geostrophic solution [Muraki and Snyder, 2007], Wang et al. [2009] inverted antisymmetric PV anomalies using the nonlinear balance equations [Davis and Emanuel, 1991], Viúdez [2007] used an original inversion method and a unique code having PV as a prognostic variable [Dritschel and Viúdez, 2003; Viúdez and Dritschel, 2003].

In all cases, a robust phenomenology emerged from these simulations: after an initial adjustment, the dipoles propagated steadily and for long periods (tens of days), along trajectories that curve with a radius of curvature very large relative to the dipole size. Hence, on a timescale of a few inertial periods, the flow in the frame moving with the dipole can be considered as stationary. An inertia-gravity wave packet \( (f < \omega < 2f) \)
was systematically found in the front of the dipole, in the jet exit region, with phase lines rather normal to the jet and wavelengths contracting to smaller scales in the front of the wave packet (see Figure 13). In these diverse simulations, the presence, orientation, and relation to the background flow is strikingly robust, making these Jet Exit Region Emitted (JEREmi) waves a paradigm to understand similar wave packets found in baroclinic life cycles. The origin of the waves has been carefully examined and discussed, demonstrating unambiguously that they are not remnants of the adjustment of the initial condition but truly result from spontaneous generation [Snyder et al., 2007; Wang and Zhang, 2010]. Vertical cross sections through the dipole axis clearly suggest that the waves originate in the jet core, where fluid parcels undergo significant acceleration then deceleration, accompanied with vertical displacements [McIntyre, 2009]. The waves are then a conspicuous component of the flow in the jet exit region, consistent with wave-capture (Bühler and McIntyre [2005] and section 4.3). This effect of the background deformation and shear can be seen graphically from the tendency of the phase lines to align with the isolines of along-jet velocity (Figure 13 or Wang et al., 2009, Figure 14b) and was verified using ray tracing by Wang et al. [2010]. This was discussed independently by Viúdez [2008], yielding the same conclusion. The waves were found not to be detectable when the Rossby number was too small (less than 0.15 [Snyder et al., 2007] or less than 0.05 [Wang et al., 2009]) and showed an algebraic dependence above that (exponents between 2 and 6). The dependence on the Rossby number however is very sensitive to resolution [Wang et al., 2009] and is obtained only for a narrow range of Rossby numbers (e.g., 0.15–0.30 in Snyder et al. [2007])). Hence, this dependence could not be conclusively compared with theoretical predictions.

Because the waves have rather small amplitudes, they can be explained as a linear response to a forcing which is akin to the imbalance in the flow. The idea of such a linearization goes back, in the context of frontogenesis, at least to Ley and Peltier [1978], Snyder et al. [1993], and Reeder and Griffiths [1996]. A framework for such linearization adapted to JEREmi waves has been discussed by Plougonven and Zhang [2007], emphasizing the need to linearize around the large-scale background flow. The main assumption is that the waves are a small perturbation, so that it makes sense to decompose the flow into a large-scale balanced part and a perturbation. As a crude sketch of this linearization, we consider the equation for the velocity in the $x$ direction, $u$, in the Boussinesq approximation on the $f$-plane [e.g. McWilliams and Gent, 1980]:

$$\frac{\partial u}{\partial t} + u \nabla u - f v + \frac{\partial \Phi}{\partial x} = 0,$$

where $f$ is the Coriolis parameter and $\Phi$ is geopotential. Now, the flow can always be decomposed into two components $u = \bar{u} + u'$, where $\bar{u}$ is a balanced approximation of the flow (or its large-scale part) and $u'$ the residual, including gravity waves and higher-order balanced corrections. Injecting the decomposition into (9), three types of terms appear: terms involving only the balanced flow are moved to the right-hand side (rhs), terms linear in the perturbations are kept on the lhs, and terms that are quadratic in perturbations...
are neglected. This yields forced equations for the perturbations $u'$, linearized on the background balanced flow $\bar{u}$:

$$\frac{\partial u'}{\partial t} + \bar{u} \nabla u' + u' \nabla \bar{u} - f v' + \frac{\partial \Phi'}{\partial x} = F_u,$$

where

$$F_u = \frac{\partial \bar{u}}{\partial t} + \bar{u} \nabla \bar{u} - f \bar{v} + \frac{\partial \Phi}{\partial x},$$

is the residual tendency; i.e., the residual when the balanced solution is injected into the primitive equations. The choice of a balanced relation may cancel some but not all of the residual tendencies ($F_u$, $F_v$, $F_\\bar{u}$). Note that if used in a systematic asymptotic approach with $Ro \ll 1$, the above yields no emission [Reznik et al., 2001; Vanneste, 2008; Plougonven et al., 2009]. Emission appears at finite $Ro$, when the advection on the lhs and the forcing on the rhs are both strong enough.

Several studies have simulated such linear equations with a forcing deduced from knowledge of the balanced dipole [Snyder et al., 2009; Wang et al., 2010; Wang and Zhang, 2010]. They demonstrated that the structure (location, orientation, intrinsic frequency) of the wave-packet is mainly determined by the background flow, i.e., the lhs operator, rather than by the forcing. In other words, and as supported using ray tracing, “the effects of propagation dominate over the source” [Wang et al., 2010]. This should not be taken as ruling out the importance of the forcing, which not only determines the amplitudes of the emitted waves, but also selects a certain range of excited frequencies [Wang and Zhang, 2007; Lin and Zhang, 2008; Wang and Zhang, 2010]. This linearization around a balanced, background flow has also been used to explain at least some of the jet-exit region gravity waves found in baroclinic life cycles [Wang, 2008].

This linearization is in part inspired by Ford’s work on Lighthill radiation [Reeder and Griffiths, 1996; Plougonven and Zhang, 2007]. Essential differences need to be emphasized to avoid confusion: in the case of Lighthill radiation, the scale separation between the vortical flow and the GW implies that the lhs operator is that for GW on a background of fluid at rest [Plougonven and Zhang, 2007; Plougonven et al., 2009]. One important consequence is that the quadrupolar form of the forcing partly determines the weakness of the emission [Ford et al., 2000, 2002]. For JEREmi waves, the scale separation is the opposite, implying that the background flow is not at rest. Consequently, advection plays a crucial role in allowing the forcing to project onto fast intrinsic timescales. The higher-order derivatives of the large-scale forcing enhances the small-scale part of the forcing, and hence this projection. Fundamental conclusions regarding Lighthill radiation [Ford et al., 2002] no longer hold, and this motivates a sharp distinction between the generation mechanism at play in stratified dipoles or baroclinic life cycles and Lighthill radiation [Zhang, 2004; McIntyre, 2009].

In summary, different dipole experiments have shown the robustness of Jet Exit Region Emitted (JEREmi) waves. The crucial ingredients are strong velocities in the jet core, combined with along-jet variations: the first leads to strong advection (e.g. $\bar{u} \nabla u'$), the second produces a forcing (a zonally symmetric jet does not by itself produce waves). The advection allows this forcing to project onto fast Lagrangian timescales (shorter than $1/f$). This explanation of low-frequency waves found in jet exit regions is a significant advance, given that such waves have frequently been described in case studies (see section 2.2). It emphasizes the role of wave capture, which has been identified also in idealized baroclinic life cycles [Plougonven and Snyder, 2005]. In the simplified configuration of steadily propagating dipoles, the waves appear captured in the sense that they do not leak upward into the fluid above (see Figure 13). In more realistic flows, simulations suggest that significant leakage should be expected [Plougonven and Snyder, 2005; Waite and Snyder, 2009], and observational studies suggest that the presence of strong winds above (e.g., the Polar Night Jet) are favorable [Tateno and Sato, 2008].

A final remark is in order here: it is assumed above that the balanced dipole is not an exact solution of the primitive equations. Indeed, although steadily propagating dipoles have been obtained in shallow water as exact solutions [Kizner et al., 2008], it is unlikely that exact solutions of dipoles can be found in the continuously stratified case. This opinion is based on the assumptions necessary to obtain solutions in shallow water, the different dispersion relation in a continuously stratified fluid, and direct numerical simulations of the dipolar solutions found in shallow water [Ribstein et al., 2010]. The issue remains open.
6. Impacts and Parameterizations

A major motivation driving recent research on atmospheric gravity waves is their role in transferring momentum toward the middle atmosphere [Fritts and Alexander, 2003]. Constraints from observations and simulations, along with a better physical understanding, are needed to improve parameterizations in Atmospheric General Circulation Models (GCMs) (section 6.1). Yet gravity waves emitted from atmospheric jets and fronts also matter for other impacts, such as their local contributions to mixing and turbulence (section 6.2), and also to temperature-dependent phenomena (section 6.3). While all the studies described above focus on the atmosphere, the same dynamical mechanisms that have been discussed in sections 3 and 5 are also active in the ocean, as discussed in section 6.4.

6.1. Momentum Fluxes and Parameterizations

Gravity waves are crucial to the general circulation of the stratosphere and mesosphere because they transfer momentum upward [Andrews et al., 1987]. Atmospheric general circulation models (GCMs) typically include two parameterizations, one for orographic gravity waves and one for nonorographic gravity waves. The latter generally have an arbitrarily fixed source at a given level, tuned in order to produce a reasonable stratospheric circulation [Kim et al., 2003]. While parameterizations of convective sources of gravity waves have been elaborated and implemented in the last decade [Beres et al., 2004, 2005; Song and Chun, 2005], parameterizations of waves produced by jets and fronts remain exceptional: Rind et al. [1988] included waves generated by wind shear at the level of the tropospheric jet stream. Charron and Manzini [2002] and Richter et al. [2010] have used the frontogenesis function [Miller, 1948; Hoskins, 1982] in the midtroposphere (600 hPa) as a diagnostic to identify active source regions. Richter et al. [2010] prescribed the emitted waves with a Gaussian phase speed spectrum centered on the local wind, and kept the amplitudes as a tunable parameter. Improvements included a reduction of the cold pole bias and a better variability of the stratospheric circulation (frequency of Stratospheric Sudden Warmings), although other changes to the code also contributed to these improvements.

Implementing successfully a new parameterization with variable sources, without degrading other features of the GCM’s circulation, is already a significant achievement. Yet, the parameterizations described above remain heuristic, and progress is needed to include more physical understanding. Pathways to improve parameterizations of jets and fronts as sources include the systematic use of observational data sets (e.g., Gong et al. [2008] for radiosonde observations), numerical modeling (e.g., Zülicke and Peters, 2006) and theoretical developments (e.g., Lott et al., 2010). Zülicke and Peters [2008] have elaborated a parameterization of inertia-gravity wave generation in poleward-breaking Rossby waves, using the cross-stream Lagrangian Rossby number as a central quantity to diagnose emission. Mesoscale simulations and observations of ten cases were used to justify their approach.

Motivation to render the nonorographic sources more realistic (e.g., variable in time and space) includes evidence from studies of GW sources and needs from GCM modeling: different lines of evidence (idealized simulations [Sato et al., 2009], balloon observations [Hertzog et al., 2008] and real-case simulations [Plougonven et al., 2013]) point to oceanic regions in the midlatitudes (i.e., to nonorographic GW sources) as significant sources. Regarding modeling, it is evidently unsatisfactory and unphysical not to link emitted waves to the flow that is exciting them. In practice, the poor representation of gravity waves has been emphasized as a likely cause of important biases in GCMs [Pawson et al., 2000; Austin et al., 2003; Eyring et al., 2007; Butchart et al., 2010]. Yet more fundamentally, Haynes [2005] concludes his review of stratospheric dynamics by emphasizing that “further (and possibly greater) potential uncertainty enters through the extreme difficulty in simulating possible changes in gravity wave sources in the troposphere.”

6.2. Transport, Mixing, and Turbulence

Gravity waves contribute in several ways to transport and mixing. Danielsen et al. [1991] proposed, based on the analysis of airborne measurements, that the differential advection due to a low-frequency, large scale wave can induce laminar structures, favoring cross-jet transport and mixing. Irreversible mixing is then achieved by smaller-scale gravity waves when they break. Pierce and Fairlie [1993] thus suggested that inertia-gravity waves contribute to transport across the edge of the polar vortex, but called for further investigation for this effect to be quantified. Observational evidence for the production of laminae by inertia-gravity waves has been described by Teitelbaum et al. [1996] and Pierce and Grant [1998]. In another case study explicitly addressing this process, Tomikawa et al. [2002] found the contribution of inertia-gravity waves to be negligible.
In the numerical simulations of O’Sullivan and Dunkerton [1995], significant anomalies tied to inertia-gravity waves appeared in plots of the potential vorticity near the tropopause, which were interpreted as a signature of transport. Moustouei et al. [1999] argued, based on observations and the numerical results of O’Sullivan and Dunkerton [1995], that gravity waves could promote cross-tropopause mixing.

In summary, there is evidence that inertia-gravity waves can produce laminae, which promote mixing. However, quantifying such contributions of gravity waves to mixing remains an issue.

On smaller scales, the breaking of gravity waves produces mixing and turbulence [e.g., Fritts et al., 2003]. The latter is of importance for aviation and forecasting of turbulence Sharman et al. [2006, 2012]. It is of particular importance to predict occurrences of clear-air turbulence (CAT), and the tropopause region near the jet stream is a major source of CAT events [e.g., Kim and Chun, 2011]. Now, case studies have proven inertia-gravity waves in the vicinity of the jet-stream to be one mechanism leading to CAT [Lane et al., 2004; Koch et al., 2005] by locally enhancing shear. Knox et al. [2008] claimed to predict CAT from jet-generated IGWs as an application of Lighthill radiation, yet for several reasons Lighthill radiation here does not apply [Plougonven et al., 2009; Knox et al., 2009]. In fact, further investigation of this case [Trier et al., 2012] has recently showed that gravity waves due to convection were mostly responsible for the turbulence events analyzed by Knox et al. [2008].

6.3. Temperature Dependent Phenomena
Propagating gravity waves induce reversible temperature fluctuations. These can be of importance for phenomena that depend nonlinearly on temperature, and particularly those with a threshold. High-frequency waves, as generated from convection and orography, will be most efficient in producing substantial temperature fluctuations, yet inertia-gravity waves have also been found to contribute.

At high latitudes, gravity waves contribute in this way to polar stratospheric clouds (PSCs). Orographic waves are a priori the main source of waves involved [Carslaw et al., 1998] and for which clear and systematic effects have been documented and the impact on PSCs discussed [e.g., Dörnbrack et al., 2002; Hertzog et al., 2002b; Mann et al., 2005; Eckermann et al., 2009]. The contribution from orographic waves is well established [e.g., McDonald et al., 2009; Alexander et al., 2011] and is more emphasized than that of nonorographic waves. Yet observational case studies have shown that gravity waves generated by jets and fronts can also produce PSCs, both in the Antarctic [Shibata et al., 2003] and in the Arctic [Hitchman et al., 2003; Buss et al., 2004; Eckermann et al., 2006].

Another example is the freeze-drying of air entering the stratosphere in the Tropical Tropopause Layer [Fueglistaler et al., 2009]. Gravity waves contribute to temperature fluctuations that will affect the freeze-drying process [Potter and Holton, 1995; Jensen et al., 1996], but it is possible that it does not modify significantly the final water vapor mixing ratios [Jensen and Pfister, 2004]. In any case, convection is here the relevant source for the gravity waves involved.

6.4. In the Ocean
One motivation for many of the studies on the limitations of balance (section 3.3) comes from the need to understand dissipation in the ocean [Wunsch and Ferrari, 2004]. The prevalent balances (hydrostasy and geostrophy, or some form of gradient-wind balance) and the implied energy cascade to large scales implies a conundrum: what are the pathways for energy, injected by the wind forcing into geostrophic motions, toward the small-scales, where it can be dissipated [McWilliams, 2003]? Interaction of balanced motions with internal gravity waves and inertial oscillations constitutes one possible route [Müller et al., 2005]. Several studies of unbalanced instabilities have been undertaken to quantify the efficiency of this route (e.g., Molemaker et al. [2005] and references therein). Recent high-resolution numerical simulations, both idealized [Molemaker et al., 2010] and realistic [Capet et al., 2008a, 2008b], have rather emphasized the appearance, at short scales, of frontal instabilities. Such instabilities are however absent from other high-resolution simulations of upper ocean geostrophic turbulence [Klein et al., 2008], calling for further investigation. Now, while internal waves or inertial oscillations may play a role in the forward energy cascade leading to dissipation, it is those forced by other mechanisms, particularly winds, that are likely involved [Gertz and Straub, 2009]. In both cases, the focus has moved away from spontaneously generated gravity waves.

Danioux et al. [2012] have recently investigated specifically the spontaneous generation of waves from upper ocean turbulence in an idealized setting. Surface quasi-geostrophy (SQG) captures well the dynamics of the baroclinically unstable current and the turbulent mesoscale and submesoscale eddy field. In partic-
ular, SQG leads to large Rossby numbers at small scales [Juckes, 1994], and hence spontaneous generation. The generation is very localized (i.e., very intermittent spatially), which is consistent with an exponential dependence on Rossby number. Once generated however, the waves contribute to a more homogeneously distributed gravity wave field at depth, where the flow is much weaker. This generation is small (the energy in the gravity waves is $10^5$ times weaker than the energy in the balanced flow) in comparison to inertia-gravity waves generated by winds [e.g., D'Asaro et al., 1995]. The generation occurs near the grid-scale, and further investigations will be necessary to assess more firmly the intensity and realism of such generation.

Polzin [2008, 2010] has argued that wave-capture was playing a role in the ocean, and more generally that the consideration of horizontally varying background flows fundamentally modifies interactions between waves and the mean flows. However, detailed evidence for the occurrence of wave capture in the ocean is still lacking. Observation and simulations of this faces one major difficulty in the ocean: near the surface, the major source of near-inertial motions are the surface winds, forcing large-scale motions (several hundreds to a thousand kilometers) that are then distorted by the mesoscale, balanced vortices (scales of ten to a few hundred kilometers) to finer and finer scales [Young and Jelloul, 1997; Klein and Smith, 2001]. If waves undergoing capture are present, it will be at scales smaller than those of the mesoscale vortices, with amplitudes probably weaker than the wind-forced near-inertial oscillations, making them difficult to observe and simulate.

7. Discussion and Perspectives

Current knowledge from observations, theory and modeling studies on internal gravity waves emanating from jets and fronts has been reviewed. Below we discuss to what extent the different threads of investigation tie up together to provide a comprehensive understanding. Focusing on generation mechanisms, we summarize salient points, emphasize limitations so as to determine, critically, what should be preserved as robust conclusions, and identify what open questions constitute essential challenges.

7.1. On Generation Mechanisms

The generation mechanism that has most often been invoked is geostrophic adjustment (section 3.1), not only in observations [Kaplan et al., 1997; Pavelin et al., 2001; Plougonven et al., 2003] but also in numerical simulations [O’Sullivan and Dunkerton, 1995] and sometimes in analytical studies [Fritts and Luo, 1992].

We wish to emphasize that the recurrent reference to geostrophic adjustment turns out to be unhelpful and argue that it should be avoided. It gives the misleading impression that there is, readily available, a theoretical paradigm for understanding the emission of gravity waves by jets and fronts, with foundations going back several decades to the work of Rossby [1938]. We argue that studies of geostrophic adjustment are in fact unhelpful for three reasons: (1) They take the imbalance as part of a given initial condition, hence circumventing the essential difficulty, i.e., to understand how, why, and where this imbalance is produced. (2) The background flows for which the adjustment problem is well posed theoretically and for which results are available are simple flows: axially or zonally symmetric, or with small Rossby number $Ro \ll 1$. Relevant flows in practice are more complex (with spatial and temporal variations, locally large $Ro$). (3) The classical scenario (imbalance propagating away as IGW, leaving a balanced flow behind) is valid only for the simple configurations aforementioned. This does not describe the phenomena observed and simulated near jets and fronts, where the emission is continuous, and no simple final adjusted state can be identified.

Now, it is true also that the notion of geostrophic adjustment can be extended, e.g., to include adjustment of perturbations on a background flow [Van Tuyl and Young, 1982; Plougonven and Zeitlin, 2005]. It can be stretched to describe the response to arbitrary, time-dependent injection of imbalance [Weigel and Lin, 1997; Chagnon and Bannon, 2005a, 2005b]. The traditional initial condition problem is then a particular case, with a forcing that is a Dirac $\delta$ function of time. With such a generalized definition however, geostrophic adjustment loses its precise meaning and encompasses all linear responses to a prescribed forcing, for instance, convectively generated waves (diabatic forcing). Hence, we prefer to preserve a precise meaning for geostrophic adjustment and continue below to use it in its traditionally accepted form (section 3.1).

In summary, geostrophic adjustment has been repeatedly invoked as the mechanism responsible for emission near jets and fronts, partly through lack of a better explanation and partly because of the presence of a strong, large-scale imbalance in the vicinity of the waves. The following picture, generalizing the notion
of adjustment, has guided intuition: the nonlinear evolution of a balanced flow leads to the appearance and growth of localized regions of imbalance. This imbalance partly projects onto gravity waves. The “production” of imbalance may persist, so that the flow does not appear to adjust; i.e., the imbalance does not decrease and disappear (at least not on timescales of a few inertial periods) and gravity waves are continuously emitted. Now this phenomenology, as found in case studies (section 2.2) or in idealized experiments (section 5), differs from that described by classical geostrophic adjustment: first, the emission takes place continuously in time, not just in a short initial period. Second, the imbalance is not found to decay after the appearance of waves; for instance, it is stationary in the dipole. Concomitantly, the flow does not evolve simply to a balanced state that can be predicted in advance; e.g., in baroclinic life cycles, the flow continues its complex, nonlinear evolution which comprises imbalance. Third, the waves do not necessarily propagate away; for example, waves emitted in the dipole remain as an inherent part of the dipole. In baroclinic life cycles, only part of the waves generated near the upper level jet leak away into the stratosphere. Hence, we believe it is preferable to distinguish the emission by jets and fronts from geostrophic adjustment (McIntyre [2001], p1723 and 1731). Keeping the term “adjustment” (because of the guiding image sketched above, which generalizes adjustment to a situation where the imbalance is continuously forced), we advise to use the terms spontaneous adjustment emission [Ford et al., 2000; Viúdez and Dritschel, 2006; Wang and Zhang, 2010], or simply spontaneous emission.

Over the past two decades, substantial progress has been achieved in understanding and quantifying how balanced motions may create imbalance and gravity waves spontaneously [Vanneste, 2013]. We first summarized mechanisms for spontaneous emission that have been identified analytically (section 3). Lighthill radiation (section 3.2), which has been very inspiring as the first clear mechanism of gravity wave emission from balanced motions, explains waves that have spatial scales larger than the balanced flow (with \( Ro > 1 \)) generating them. It is useful to explain waves generated from intense vortices such as cyclones and mesocyclones [Scher, 2008]. Unbalanced instabilities and transient generation (sections 3.3 and 3.4) describe how shear couples gravity waves and balanced motions, leading to emission in the form of unstable modes or transient bursts. These have scales comparable to or somewhat larger than the Potential Vorticity (PV) anomalies that are sheared. In all three mechanisms, emission occurs when and where the appropriate scales (timescales and spatial scales) match: the scales of the balanced flow and the scales of potential inertia-gravity waves, i.e., consistent with the dispersion relation. In the configurations most relevant to jets and fronts (plane parallel sheared flows), studies have emphasized the importance of differential advection (i.e., shear) for coupling balanced motions and gravity waves: the slow, balanced motions connect to fast gravity wave motions thanks to Doppler shifting. Finally, note that there are many connections between these different mechanisms (sections 3.2, 3.3, and 3.4). For instance, some unbalanced instabilities can be described as Lighthill radiation.

The range of applicability of these mechanisms remains to be evaluated, but two points are worth noting: first, unbalanced instabilities have been difficult to exhibit in dedicated laboratory studies because of their weakness (weak growth rates and/or low level of saturation, see section 5.1). Second, the coupling of gravity waves and PV anomalies in shear may be more relevant for other flow configurations, where other processes such as wave-breaking produce small-scale PV anomalies that are subsequently sheared. In other words, these theoretical mechanisms for the spontaneous generation of gravity waves from balanced motions have not, so far, been found to apply and explain the emission of waves from jets and fronts in real cases, making it necessary to consider more complex flows.

7.2. Jet Exit Region Emitted (JERem) Waves

One remarkable outcome from observations and numerical modeling has been the robustness of the paradigm put forward by Uccelini and Koch [1987], and the dynamical understanding obtained since. Observational case studies (sections 2.2) and idealized simulations (5.3 and 5.4) have emphasized jet exit regions, upstream of a ridge and also, less frequently, of a trough, as a favored location for large-amplitude, subsynoptic inertia-gravity waves (see section 2.2 and Figure 4). The convergence of different approaches and the recurrence of this configuration in numerous studies are indications of the robustness of this result.

Theory has highlighted propagation effects, namely “wave-capture”, as a mechanism enhancing IGW in such a region of the flow (section 4.3), the large-scale strain and vertical shear determining certain of the wave characteristics. Simulations of idealized baroclinic life cycles (section 5.3) have also highlighted jet exit regions (see Figures 10 and 11). A further simplification of the flow has consisted in restricting to dipoles, i.e.,
coherent structures that include a local wind maximum and that have a nearly steady propagation. Several different modeling studies have robustly identified a low-frequency wave packet in the front of the dipole, with characteristics consistent with wave capture, as an inherent part of the dipoles, steadily propagating with them (see Figure 13). The emission mechanism has been explained as the linear response to the differences between the balanced and the full tendencies (see section 5.4). The key point is that the dynamics are linearized on the background of an approximation of the dipole. The forcing is also deduced from this approximate, balanced dipole. The response is not very sensitive to the specific shape of the forcing but rather to the background flow used in the linearization.

The explanation of waves found in dipoles is an encouraging result, because of the similarity of these JEREmi (Jet Exit Region Emitted) waves with waves identified in more complex, idealized flows (section 5.3), and of the similarity of these latter waves with those described in observational studies (section 2.2). Nonetheless, revisiting observations with the understanding gained from theory and idealized simulations remains largely to be done in order to assess: (1) How systematic is the presence of such waves in atmospheric jet exit regions? (2) Why are amplitudes found in idealized simulations weaker than those observed? (3) How efficient is the capture mechanism, or in other words what proportion of the waves leak upward to the middle atmosphere? (4) How important are these waves for the general circulation relative to other waves present in the vicinity of jets and fronts? A further, fundamental issue is (5) to understand the impact on the large-scale flow of these waves and their interaction with a horizontally varying flow [Bühler and McIntyre, 2005].

Present understanding on JEREmi waves can nonetheless lead to certain suggestions to improve parameterizations of nonorographic waves in midlatitudes, relative to a constant source. Robust results concern the orientation of the waves (phase lines parallel to the extensional axis of the local deformation field where the latter is intense), their intrinsic frequency (set by the deformation and vertical shear, and typically between $f$ and $2f$) and their phase speeds (close to the phase speed of the baroclinic waves, between 10 and 20 $\text{m s}^{-1}$). Regarding the location of the waves, considering only jet exit regions may be too restrictive (in idealized simulations at late times, the whole region of the jet is populated with waves [Waite and Snyder, 2009]).

Diagnosing regions of emission by diagnostics that highlight cyclogenesis, frontogenesis, strong jet curvature is qualitatively justified, though there is no rigorous basis for a quantitative relation. Strong shear between the tropospheric jet-front system and the lower stratospheric flow may also be of relevance. Identifying regions of large-scale imbalance is informative, but should be complemented with the identification of regions of strong advection. Regarding the amplitudes of the emitted waves, it seems that there remains too much of a discrepancy between the amplitudes of waves in idealized simulations and those in observational case studies to conclude.

### 7.3. Waves From Other Processes

JEREmi waves are not the only waves present in the vicinity of jets and fronts, there are other potential sources of gravity waves near jets and fronts: first, extant idealized modeling studies have simulated a richer array of gravity waves, e.g., with waves emanating from surface fronts (sections 5.2 and 5.3). Second, these simulations have focused on early times. Third, they have limitations such as the absence of moist processes or of a boundary layer. The parameterizations of these small-scale processes have their own uncertainties, yet these processes are of great importance: for instance, diabatic heating acts directly on the buoyancy and at small-scales, and is therefore a very efficient forcing for gravity waves. Case studies have recurrently mentioned the possible important role of moisture (see section 2.2). Addition of moisture in idealized baroclinic life cycles will have a priori two implications: one is to accelerate and intensify the development of baroclinic instability [e.g., Waite and Snyder, 2012], which should enhance the excitation of gravity waves through spontaneous generation [Reeder and Griffiths, 1996; Wang and Zhang, 2007]. The other is to excite, through moist convection, additional waves. Those produced on small-scales from convective cells should have strikingly different characteristics (short horizontal wavelengths (tens of km), long vertical wavelengths (5-10 km), and correspondingly high intrinsic frequencies). On the other hand, the large scale envelope of convection will also contribute to the gravity wave field on a larger scale, and this contribution will be more difficult to isolate. Simulations of moist baroclinic life cycles indeed suggest a much more energetic gravity wave field than in dry simulations [Waite and Snyder, 2012; Mirzaei et al., 2013; Wei and Zhang, 2013].

Idealized moist simulations will contribute to guiding our understanding, as they have for the impacts of moisture on the predictability of mesoscale weather [Zhang et al., 2007], but they necessarily involve
parameterizations of convective and boundary layer processes, which are themselves quite uncertain. The implication is that further studies of moist generation of gravity waves from fronts will call strongly for observational constraints. Combined studies involving both simulations and observations should be an important step to provide a complete description of waves near moist fronts [Zhang et al., 2011].

In a similar vein, additional complexity relative to idealized baroclinic life cycles may come from the generation of gravity waves from small scale turbulent motions, e.g., emission from shear instability. Previous studies on the subject have conclusively ruled out a straightforward, linear connection, but studies of the nonlinear development of the shear instability have shown that this mechanism although relatively weak should be considered as a source of gravity waves (section 3.5). Yet, the numerical configurations used remained quite idealized. Here again, observations will play a key role in constraining the realism of numerical simulations. A fundamental difficulty here again is the complexity of the background flow, involving a wide range of scales from the synoptic motions to the small-scale turbulence.

**7.4. Perspectives**

Now, both points above have emphasized the complexity that will be encountered in exploring gravity waves generated by jets and fronts as one explores finer scales. Moist convection and small-scale turbulence are themselves challenges for modeling and observation. It will likely be impossible to draw a simple, deterministic and convincing picture of the way gravity waves are generated from these processes in a complex flow environment such as a cold front within a baroclinic wave. Yet, the demand from applications (parameterizations for GCMs, forecasting of turbulence) may not call for such a deterministic picture. Observations should play a key role (see also challenges discussed in section 2.3). Global high-resolution data sets have been obtained, and the combined use of different observational platforms along with modeling promises to provide global descriptions of the gravity wave field in coming years [Geller et al., 2013]. We believe one way forward will be to analyze such high-resolution data sets to produce flow-dependent characterizations of gravity waves (e.g., rather than quantify the mean GW activity at a given location, quantify it relative to flow configuration). This can bring practical answers to the needs of climate and forecast models. Presently, GCMs that include a parameterization of nonorographic waves are the exception, and there is much room for improving on the heuristic relation used to connect the emitted waves to the tropospheric flow (section 6.1). The trend toward stochastic parameterizations [Palmer, 2001; Eckermann, 2011; Lott et al., 2012b] is in phase with new descriptions of the gravity wave field [Hertzog et al., 2012].

The perspective of quantifying jets and fronts as sources of gravity waves, and hence of measuring and parameterizing their variability, will make GCMs more physical, and should improve their internal variability. It will also set the stage for investigations of the variability of this forcing, of its evolution in a changing climate and of the implications, as questioned by Haynes [2005] (see section 6.1).

**Glossary**

*Balanced model:* approximate model that relies on balance relations which diagnostically relate several variables (e.g., velocity and pressure in geostrophic balance) to simplify the dynamics. The evolution of the flow typically reduces to one equation (conservation of Potential Vorticity), and the balance relations (e.g., hydrostasy and geostrophy for the quasi-geostrophic approximation) make it possible to invert the Potential Vorticity to recover all fields, and in particular the velocity (see Hoskins et al. [1985], and section 3.2).

*Baroclinicity:* measure of how the isoflows of the density field and of the pressure field are misaligned. In the atmosphere, baroclinicity is strongest where there are strong horizontal thermal gradients, as in midlatitudes, and is associated to vertical shear through thermal wind balance (e.g., Holton, 1992).

*Inertia-gravity wave:* gravity wave having a low frequency (close to the lower bound of the gravity wave spectrum, i.e., \( f \) the Coriolis parameter). See section 1.

*Intrinsic frequency:* frequency in the frame moving with the fluid. The intrinsic frequency \( \dot{\omega} \) is related to the ground-based frequency \( \omega \) by \( \dot{\omega} = \omega - k \mathbf{U} \), where \( k \) is the wave number and \( \mathbf{U} \) is the background wind (see section 4).

*Lighthill radiation:* James Lighthill pioneered the description of the emission of acoustic waves by turbulent motions in a compressible fluid [Lighthill, 1952]. His analysis, carried out for small Mach number, can be applied in the geophysical context to describe the emission of gravity waves by balanced motions if the latter have a Rossby number of order unity. The application to the geophysical context is due to Rupert Ford [e.g., Ford, 1994a; Ford et al., 2000] and is sometimes called Ford-Lighthill emission.
**Polar Night Jet**: intense westerly jet that forms in the winter stratosphere, at high latitudes (typically 60°) and altitudes higher than 20 km. It encloses the polar vortex, and isolates it from midlatitude air.

**Rossby number**: ratio $U/fL$, where $U$ is a typical order of magnitude for wind velocity, $L$ is a typical horizontal scale, and $f$ is the Coriolis parameter. This compares the advective timescale $L/U$ with the inertial timescale $1/f$, and is typically small at midlatitudes for synoptic scales.

**Superpressure balloons**: balloons used for atmospheric measurements, with an envelope that is not extendable. At the level where the balloons drift, the gas inside has a pressure larger than the environment, so that the balloon remains fully inflated and the full device has a constant density. It therefore drifts along an isopycnic surface, and may be considered a quasi-Lagrangian tracer (see Hertzog et al. [2007] and section 2.1).

**Unbalanced instabilities**: instabilities in a rotating fluid that involve unbalanced motions. These are of interest in regimes where balance is expected or even dominant (e.g., weak Rossby number), and hence the term preferentially refers to instabilities that couple balanced and unbalanced motions (section 3.3).

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